

Package ‘odr’

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Type Package

Title Optimal Design and Statistical Power of Multilevel Randomized Trials

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Description Calculate the optimal sample allocation that minimizes the variance of treatment effect in multilevel randomized trials under fixed budget and cost structure, perform power analyses with and without accommodating costs and budget. The references for proposed methods are:

(1) Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials. (unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

(2) Shen, Z., & Kelcey, B. (revise & resubmit).

Optimal sample allocation accounts for the full variation of sampling costs in cluster-randomized trials.

Journal of Educational and Behavioral Statistics.

(3) Shen, Z., & Kelcey, B. (2018, April). Optimal design of cluster randomized trials under condition- and unit-specific cost structures. Roundtable discussion presented at American Educational Research Association (AERA) annual conference.

(4) Champely, S. (2018). pwr: Basic functions for power analysis (Version 1.2-2) [Software]. Available from <<https://CRAN.R-project.org/package=pwr>>.

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odr-package	<i>Optimal Design and Statistical Power of Multilevel Randomized Trials</i>
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Description

This package is to help researchers design cost-efficient multilevel randomized trials with adequate statistical precision by (1) solving optimal sample allocations, (2) comparing design precision and efficiency between different sample allocations, and (3) explicitly accommodating costs and budget in power analyses.

Details

The package covers seven types of trials with continuous outcomes and these trials are individual randomized controlled trials (RCTs), two-, three-, and four-level cluster-randomized trials (CRTs), and two-, three-, and four-level multisite randomized trials (MRTs). There are two categorical functions for each type of trial and a uniform function for all types of trials. The two categorical functions are 'od' and 'power'. The 'od' function can calculate the optimal sample allocation with and without a constraint(s) for each type of trial. The optimal design parameters in 'od'

function include the sample sizes at each level and proportion of units to be assigned to the treatment condition. The 'power' function by default can calculate required budget (and required sample size) for desired power, minimum detectable effect size (MDES) under a fixed budget, statistical power under a fixed budget. The 'power' function also can perform conventional power analyses (e.g., required sample size, power, MDES calculation). The uniform function 're' (or 'rpe') is to compare the relative (precision and) efficiency between two designs with different sample allocations.

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od.1 *Optimal sample allocation calculation for individual randomized controlled trials*

Description

The optimal design of individual randomized controlled trials (RCTs) is to choose the sample allocation that minimizes the variance of treatment effect under fixed budget and cost structure. The optimal design parameter is the proportion of individuals to be assigned to treatment (p).

Usage

```
od.1(p = NULL, r12 = NULL, c1 = NULL, c1t = NULL, m = NULL,
     plots = TRUE, plim = NULL, varlim = NULL, plab = NULL,
     varlab = NULL, vartitle = NULL, verbose = TRUE)
```

Arguments

<code>p</code>	the proportion of individuals to be assigned to treatment.
<code>r12</code>	the proportion of outcome variance explained by covariates.
<code>c1</code>	the cost of sampling one unit in control condition.
<code>c1t</code>	the cost of sampling one unit in treatment condition.
<code>m</code>	total budget, default value is the total costs of sampling 60 individuals across treatment conditions.
<code>plots</code>	logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
<code>plim</code>	the plot range for p , default value is $c(0, 1)$.
<code>varlim</code>	the plot range for variance, default value is $c(0, 0.05)$.
<code>plab</code>	the plot label for p , default value is "Proportion of Individuals in Treatment: p ".
<code>varlab</code>	the plot label for variance, default value is "Variance".
<code>vartitle</code>	the title of variance plot, default value is NULL.
<code>verbose</code>	logical; print the value of p if TRUE, otherwise not; default value is TRUE.

Value

unconstrained or constrained optimal sample allocation (p). The function also returns the variance of treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2))
myod1$out # output

# constrained p, no calculation performed #-----
myod2 <- od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2), p = 0.5)
myod2$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.87

# when sampling costs are equal, a balanced design with p = 0.5 is the best #-----
myod3 <- od.1(r12 = 0.5, c1 = 1, c1t = 1, varlim = c(0, 0.2))
myod3$out # output
```

Description

The optimal design of two-level cluster randomized trials (CRTs) is to choose the sample allocation that minimizes the variance of treatment effect under fixed budget and cost structure. The optimal design parameters include the level-1 sample size per level-2 unit (n) and the proportion of level-2 clusters/groups to be assigned to treatment (p). This function solves the optimal n and/or p with and without constraints.

Usage

```
od.2(n = NULL, p = NULL, icc = NULL, r12 = NULL, r22 = NULL,
     c1 = NULL, c2 = NULL, c1t = NULL, c2t = NULL, m = NULL,
     plots = TRUE, plot.by = NULL, nlim = NULL, plim = NULL,
     varlim = NULL, nlab = NULL, plab = NULL, varlab = NULL,
     vartitle = NULL, verbose = TRUE)
```

Arguments

n	the level-1 sample size per level-2 unit.
p	the proportion of level-2 clusters/units to be assigned to treatment.
icc	the unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	the proportion of level-1 variance explained by covariates.
r22	the proportion of level-2 variance explained by covariates.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
m	total budget, default value is the total costs of sampling 60 level-2 units across treatment conditions.
plots	logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	specify variance plot by n and/or p; default value is plot.by = list(n = "n", p = "p").
nlim	the plot range for n, default value is c(2, 50).
plim	the plot range for p, default value is c(0, 1).
varlim	the plot range for variance, default value is c(0, 0.05).
nlab	the plot label for n, default value is "Level-1 Sample Size: n".
plab	the plot label for p, default value is "Proportion Level-2 Units in Treatment: p"
varlab	the plot label for variance, default value is "Variance".
vartitle	the title of variance plot, default value is NULL.
verbose	logical; print the values of n and p if TRUE, otherwise not; default value is TRUE.

Value

unconstrained or constrained optimal sample allocation (n and p). The function also returns the variance of treatment effect, function name, design type, and parameters used in the calculation.

References

- Shen, Z., & Kelcey, B. (2018, April). Optimal design of cluster randomized trials under condition- and unit-specific cost structures. Roundtable discussion presented at American Educational Research Association (AERA) annual conference, New York City, NY;
- Shen, Z., & Kelcey, B. (revise & resubmit). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*.
- Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```

# unconstrained optimal design #-----
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             varlim = c(0.01, 0.02))
myod1$out # output
# plot by p
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             varlim = c(0.01, 0.02), plot.by = list(p = 'p'))

# constrained optimal design with n = 20 #-----
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             n = 20, varlim = c(0.005, 0.025))
myod2$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$re # RE = 0.88

# constrained optimal design with p = 0.5 #-----
myod3 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             p = 0.5, varlim = c(0.005, 0.025))
myod3$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod3)
myre$re # RE = 0.90

# constrained n and p, no calculation performed #-----
myod4 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             n = 20, p = 0.5, varlim = c(0.005, 0.025))
myod4$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod4)
myre$re # RE = 0.83

```

od.2m

Optimal sample allocation calculation for two-level multisite randomized trials

Description

The optimal design of two-level multisite randomized trials (MRTs) is to choose the sample allocation that minimizes the variance of treatment effect under fixed budget and cost structure. The optimal design parameters include the level-1 sample size per level-2 unit (n) and the proportion of level-2 unit to be assigned to treatment (p). This function solves the optimal n and/or p with and without constraints.

Usage

```
od.2m(n = NULL, p = NULL, icc = NULL, r12 = NULL, r22m = NULL,
```

```
c1 = NULL, c2 = NULL, c1t = NULL, omega = NULL, m = NULL,
plots = TRUE, plot.by = NULL, nlim = NULL, plim = NULL,
varlim = NULL, nlab = NULL, plab = NULL, varlab = NULL,
vartitle = NULL, verbose = TRUE, iter = 100, tol = 1e-10)
```

Arguments

n	the level-1 sample size per level-2 unit.
p	the proportion of level-4 clusters/units to be assigned to treatment.
icc	the unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	the proportion of level-1 variance explained by covariates.
r22m	the proportion of variance of site-specific treatment effect explained by covariates.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c1t	the cost of sampling one level-1 unit in treatment condition.
omega	the standardized variance of site-specific treatment effect
m	total budget, default is the total costs of sampling 60 level-2 units.
plots	logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	specify variance plot by n and/or p; default value is plot.by = list(n = "n", p = "p").
nlim	the plot range for n, default value is c(2, 50).
plim	the plot range for p, default value is c(0, 1).
varlim	the plot range for variance, default value is c(0, 0.05).
nlab	the plot label for n, default value is "Level-1 Sample Size: n".
plab	the plot label for p, default value is "Proportion Level-1 Units in Treatment: p".
varlab	the plot label for variance, default value is "Variance".
vartitle	the title of variance plot, default value is NULL.
verbose	logical; print the values of n and p if TRUE, otherwise not; default value is TRUE.
iter	number of iterations; default value is 100.
tol	tolerance for convergence; default value is 1e-10.

Value

unconstrained or constrained optimal sample allocation (n and p). The function also returns the variance of treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.2m(icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005))
myod1$out # n = 20, p = 0.37
# plots by p
myod1 <- od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), plot.by = list(p = 'p'))

# constrained optimal design with p = 0.5 #-----
myod2 <- od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), p = 0.5)
myod2$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.86

# constrained optimal design with n = 5 #-----
myod3 <- od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5, c1 = 1, c2 = 10,
              c1t = 10, varlim = c(0, 0.005), n = 5)
myod3$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod3)
myre$re # RE = 0.79

# constrained n and p, no calculation performed #-----
myod4 <- od.2m(icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), p = 0.5, n = 10)
myod4$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod4)
myre$re # RE = 0.84
```

Description

The optimal design of three-level cluster randomized trials (CRTs) is to choose the sample allocation that minimizes the variance of treatment effect under fixed budget and cost structure. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per

level-3 unit (J), and the proportion of level-3 clusters/groups to be assigned to treatment (p). This function solves the optimal n , J and/or p with and without constraints.

Usage

```
od.3(n = NULL, J = NULL, p = NULL, icc2 = NULL, icc3 = NULL,
     r12 = NULL, r22 = NULL, r32 = NULL, c1 = NULL, c2 = NULL,
     c3 = NULL, c1t = NULL, c2t = NULL, c3t = NULL, m = NULL,
     plots = TRUE, plot.by = NULL, nlim = NULL, Jlim = NULL,
     plim = NULL, varlim = NULL, nlab = NULL, Jlab = NULL,
     plab = NULL, varlab = NULL, vartitle = NULL, verbose = TRUE,
     iter = 100, tol = 1e-10)
```

Arguments

<code>n</code>	the level-1 sample size per level-2 unit.
<code>J</code>	the level-2 sample size per level-3 unit.
<code>p</code>	the proportion of level-3 clusters/units assigned to treatment.
<code>icc2</code>	the unconditional intraclass correlation coefficient (ICC) at level 2.
<code>icc3</code>	the unconditional intraclass correlation coefficient (ICC) at level 3.
<code>r12</code>	the proportion of level-1 variance explained by covariates.
<code>r22</code>	the proportion of level-2 variance explained by covariates.
<code>r32</code>	the proportion of level-3 variance explained by covariates.
<code>c1</code>	the cost of sampling one level-1 unit in control condition.
<code>c2</code>	the cost of sampling one level-2 unit in control condition.
<code>c3</code>	the cost of sampling one level-3 unit in control condition.
<code>c1t</code>	the cost of sampling one level-1 unit in treatment condition.
<code>c2t</code>	the cost of sampling one level-2 unit in treatment condition.
<code>c3t</code>	the cost of sampling one level-3 unit in treatment condition.
<code>m</code>	total budget, default is the total costs of sampling 60 level-3 units across treatment conditions.
<code>plots</code>	logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
<code>plot.by</code>	specify variance plot by n , J and/or p ; default is <code>plot.by = list(n = "n", J = "J", p = "p")</code> .
<code>nlim</code>	the plot range for n , default value is <code>c(2, 50)</code> .
<code>Jlim</code>	the plot range for J , default value is <code>c(2, 50)</code> .
<code>plim</code>	the plot range for p , default value is <code>c(0, 1)</code> .
<code>varlim</code>	the plot range for variance, default value is <code>c(0, 0.05)</code> .
<code>nlab</code>	the plot label for n , default value is "Level-1 Sample Size: n".
<code>Jlab</code>	the plot label for J , default value is "Level-2 Sample Size: J".
<code>plab</code>	the plot label for p , default is "Proportion Level-3 Units in Treatment: p"

varlab	the plot label for variance, default value is "Variance".
vartitle	the title of variance plot, default value is NULL.
verbose	logical; print the values of n, J, and p if TRUE, otherwise not; default is TRUE.
iter	number of iterations; default value is 100.
tol	tolerance for convergence; default value is 1e-10.

Value

unconstrained or constrained optimal sample allocation (n, J, and p). The function also returns the variance of treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (revise & resubmit). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*.

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
myod1$out # output
# plots by p and J
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025), plot.by = list(p = 'p', J = 'J'))

# constrained optimal design with J = 20 #-----
myod2 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
myod2$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.53

# constrained optimal design with p = 0.5 #-----
myod3 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, p = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
myod3$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod3)
myre$re # RE = 0.84

# constrained n, J and p, no calculation performed #-----
```

```

myod4 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, n = 10, J = 10, p = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
myod4$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod4)
myre$re # RE = 0.61

```

od.3m

Optimal sample allocation calculation for three-level multisite randomized trials

Description

The optimal design of three-level multisite randomized trials (MRTs) is to choose the sample allocation that minimizes the variance of treatment effect under fixed budget and cost structure. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), and the proportion of level-2 unit to be assigned to treatment (p). This function solves the optimal n , J and/or p with and without constraints.

Usage

```

od.3m(n = NULL, J = NULL, p = NULL, icc2 = NULL, icc3 = NULL,
      r12 = NULL, r22 = NULL, r32m = NULL, c1 = NULL, c2 = NULL,
      c3 = NULL, c1t = NULL, c2t = NULL, omega = NULL, m = NULL,
      plots = TRUE, plot.by = NULL, nlim = NULL, Jlim = NULL,
      plim = NULL, varlim = NULL, nlab = NULL, Jlab = NULL,
      plab = NULL, varlab = NULL, vartitle = NULL, verbose = TRUE,
      iter = 100, tol = 1e-10)

```

Arguments

n	the level-1 sample size per level-2 unit.
J	the level-2 sample size per level-3 unit.
p	the proportion of level-4 clusters/units to be assigned to treatment.
$icc2$	the unconditional intraclass correlation coefficient (ICC) at level 2.
$icc3$	the unconditional intraclass correlation coefficient (ICC) at level 3.
$r12$	the proportion of level-1 variance explained by covariates.
$r22$	the proportion of level-2 variance explained by covariates.
$r32m$	the proportion of variance of site-specific treatment effect explained by covariates.
$c1$	the cost of sampling one level-1 unit in control condition.
$c2$	the cost of sampling one level-2 unit in control condition.
$c3$	the cost of sampling one level-3 unit in control condition.

c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
omega	the standardized variance of site-specific treatment effect
m	total budget, default is the total costs of sampling 60 level-3 units.
plots	logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	specify variance plot by n, J and/or p; default value is plot.by = list(n = "n", J = "J", p = "p").
nlim	the plot range for n, default value is c(2, 50).
Jlim	the plot range for J, default value is c(2, 50).
plim	the plot range for p, default value is c(0, 1).
varlim	the plot range for variance, default value is c(0, 0.05).
nlab	the plot label for n, default value is "Level-1 Sample Size: n".
Jlab	the plot label for J, default value is "Level-2 Sample Size: J".
plab	the plot label for p, default value is "Proportion Level-2 Units in Treatment: p".
varlab	the plot label for variance, default value is "Variance".
vartitle	the title of variance plot, default value is NULL.
verbose	logical; print the values of n, J, and p if TRUE, otherwise not; default value is TRUE.
iter	number of iterations; default value is 100.
tol	tolerance for convergence; default value is 1e-10.

Value

unconstrained or constrained optimal sample allocation (n, J, and p). The function also returns the variance of treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005))
myod1$out # output
# plots by p and J
myod1 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
```

```

      c1t = 1, c2t = 200, c3 = 200,
      varlim = c(0, 0.005), plot.by = list(p = 'p', J = 'J'))

# constrained optimal design with p = 0.5 #-----
myod2 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), p = 0.5)
myod2$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$re # RE = 0.81

# constrained optimal design with n = 5 #-----
myod3 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), n = 5)
myod3$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod3)
myre$re # RE = 0.89

# constrained n, J and p, no calculation performed #-----
myod4 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), p = 0.5, n = 15, J = 20)
myod4$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod4)
myre$re # RE = 0.75

```

Description

The optimal design of four-level cluster randomized trials (CRTs) is to choose the sample allocation that minimizes the variance of treatment effect under fixed budget and cost structure. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), the level-3 sample size per level-4 unit (K), and the proportion of level-4 clusters/groups to be assigned to treatment (p). This function solves the optimal n , J , K and/or p with and without constraints.

Usage

```
od.4(n = NULL, J = NULL, K = NULL, p = NULL, icc2 = NULL,
     icc3 = NULL, icc4 = NULL, r12 = NULL, r22 = NULL, r32 = NULL,
     r42 = NULL, c1 = NULL, c2 = NULL, c3 = NULL, c4 = NULL,
     c1t = NULL, c2t = NULL, c3t = NULL, c4t = NULL, m = NULL,
     plots = TRUE, plot.by = NULL, nlim = NULL, Jlim = NULL,
     Klim = NULL, plim = NULL, varlim = NULL, nlab = NULL,
     Jlab = NULL, Klab = NULL, plab = NULL, varlab = NULL,
     vartitle = NULL, verbose = TRUE, iter = 100, tol = 1e-10)
```

Arguments

n	the level-1 sample size per level-2 unit.
J	the level-2 sample size per level-3 unit.
K	the level-3 sample size per level-4 unit.
p	the proportion of level-4 clusters/units to be assigned to treatment.
icc2	the unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	the unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	the unconditional intraclass correlation coefficient (ICC) at level 4.
r12	the proportion of level-1 variance explained by covariates.
r22	the proportion of level-2 variance explained by covariates.
r32	the proportion of level-3 variance explained by covariates.
r42	the proportion of level-4 variance explained by covariates.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c3	the cost of sampling one level-3 unit in control condition.
c4	the cost of sampling one level-4 unit in control condition.
c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
c3t	the cost of sampling one level-3 unit in treatment condition.
c4t	the cost of sampling one level-4 unit in treatment condition.
m	total budget, default value is the total costs of sampling 60 level-4 units across treatment conditions.
plots	logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	specify variance plot by n, J, K and/or p; default value is plot.by = list(n = "n", J = "J", K = 'K', p = "p").
nlim	the plot range for n, default value is c(2, 50).
Jlim	the plot range for J, default value is c(2, 50).
Klim	the plot range for K, default value is c(2, 50).
plim	the plot range for p, default value is c(0, 1).

varlim	the plot range for variance, default value is <code>c(0, 0.05)</code> .
nlab	the plot label for n, default value is "Level-1 Sample Size: n".
Jlab	the plot label for J, default value is "Level-2 Sample Size: J".
Klab	the plot label for K, default value is "Level-3 Sample Size: K".
plab	the plot label for p, default value is "Proportion Level-4 Units in Treatment: p".
varlab	the plot label for variance, default value is "Variance".
vartitle	the title of variance plot, default value is NULL.
verbose	logical; print the values of n, J, K, and p if TRUE, otherwise not; default value is TRUE.
iter	number of iterations; default value is 100.
tol	tolerance for convergence; default value is <code>1e-10</code> .

Value

unconstrained or constrained optimal sample allocation (n, J, K, and p). The function also returns the variance of treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
myod1$out # output
# plots by p and K
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01), plot.by = list(p = 'p', K = 'K'))

# constrained optimal design with p = 0.5 #-----
myod2 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, p = 0.5,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
myod2$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
```

```

myre$re # RE = 0.78

# constrained optimal design with K = 20 #-----
myod3 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, K = 20,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
myod3$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod3)
myre$re # RE = 0.67

# constrained n, J, K and p, no calculation performed #-----
myod4 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, n = 10, J = 10, K = 20, p = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
myod4$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod4)
myre$re # RE = 0.27

```

od.4m

Optimal sample allocation calculation for four-level multisite randomized trials

Description

The optimal design of four-level multisite randomized trials (MRTs) is to choose the sample allocation that minimizes the variance of treatment effect under fixed budget and cost structure. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), the level-3 sample size per level-4 unit (K), and the proportion of level-3 units to be assigned to treatment (p). This function solves the optimal n , J , K and/or p with and without constraints.

Usage

```

od.4m(n = NULL, J = NULL, K = NULL, p = NULL, icc2 = NULL,
      icc3 = NULL, icc4 = NULL, r12 = NULL, r22 = NULL, r32 = NULL,
      r42m = NULL, c1 = NULL, c2 = NULL, c3 = NULL, c4 = NULL,
      c1t = NULL, c2t = NULL, c3t = NULL, omega = NULL, m = NULL,
      plots = TRUE, plot.by = NULL, nlim = NULL, Jlim = NULL,
      Klim = NULL, plim = NULL, varlim = NULL, nlab = NULL,
      Jlab = NULL, Klab = NULL, plab = NULL, varlab = NULL,
      vartitle = NULL, verbose = TRUE, iter = 100, tol = 1e-10)

```


Arguments

n	the level-1 sample size per level-2 unit.
J	the level-2 sample size per level-3 unit.
K	the level-3 sample size per level-4 unit.
p	the proportion of level-3 units to be assigned to treatment.
icc2	the unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	the unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	the unconditional intraclass correlation coefficient (ICC) at level 4.
r12	the proportion of level-1 variance explained by covariates.
r22	the proportion of level-2 variance explained by covariates.
r32	the proportion of level-3 variance explained by covariates.
r42m	the proportion of variance of site-specific treatment effect explained by covariates.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c3	the cost of sampling one level-3 unit in control condition.
c4	the cost of sampling one level-4 unit.
c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
c3t	the cost of sampling one level-3 unit in treatment condition.
omega	the standardized variance of site-specific treatment effect
m	total budget, default is the total costs of sampling 60 level-4 units.
plots	logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	specify variance plot by n, J, K and/or p; default value is plot.by = list(n = "n", J = "J", K = 'K', p = "p").
nlim	the plot range for n, default value is c(2, 50).
Jlim	the plot range for J, default value is c(2, 50).
Klim	the plot range for K, default value is c(2, 50).
plim	the plot range for p, default value is c(0, 1).
varlim	the plot range for variance, default value is c(0, 0.05).
nlab	the plot label for n, default value is "Level-1 Sample Size: n".
Jlab	the plot label for J, default value is "Level-2 Sample Size: J".
Klab	the plot label for K, default value is "Level-3 Sample Size: K".
plab	the plot label for p, default value is "Proportion Level-3 Units in Treatment: p".
varlab	the plot label for variance, default value is "Variance".
vartitle	the title of variance plot, default value is NULL.
verbose	logical; print the values of n, J, K, and p if TRUE, otherwise not; default value is TRUE.
iter	number of iterations; default value is 100.
tol	tolerance for convergence; default value is 1e-10.

Value

unconstrained or constrained optimal sample allocation (n , J , K , and p). The function also returns the variance of treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
              c1 = 1, c2 = 5, c3 = 25,
              c1t = 1, c2t = 50, c3t = 250, c4 = 500,
              varlim = c(0, 0.005))
myod1$out # output
# plots by p and K
myod1 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
              c1 = 1, c2 = 5, c3 = 25,
              c1t = 1, c2t = 50, c3t = 250, c4 = 500,
              varlim = c(0, 0.005), plot.by = list(p = 'p', K = 'K'))

# constrained optimal design with p = 0.5 #-----
myod2 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
              c1 = 1, c2 = 5, c3 = 25,
              c1t = 1, c2t = 50, c3t = 250, c4 = 500,
              varlim = c(0, 0.005), p = 0.5)
myod2$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.88

# constrained optimal design with J = 20 #-----
myod3 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
              c1 = 1, c2 = 5, c3 = 25,
              c1t = 1, c2t = 50, c3t = 250, c4 = 500,
              varlim = c(0, 0.005), J = 20)
myod3$out
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod3)
myre$re # RE = 0.58

# constrained n, J, K and p, no calculation performed #-----
myod4 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
              c1 = 1, c2 = 5, c3 = 25,
```

```

      c1t = 1, c2t = 50, c3t = 250, c4 = 500,
      varlim = c(0, 0.005), p = 0.5, n = 15, J = 20, K = 5)
myod4$out
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod4)
myre$re # RE = 0.46

```

power.1	<i>Budget and/or sample size, power, MDES calculation for individual randomized controlled trials</i>
---------	---

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for individual randomized controlled trials (RCTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.1(cost.model = TRUE, expr = NULL, constraint = NULL,
        sig.level = 0.05, two.tailed = TRUE, d = NULL, power = NULL,
        m = NULL, n = NULL, p = NULL, r12 = NULL, q = NULL,
        c1 = NULL, c1t = NULL, dlim = NULL, powerlim = NULL,
        nlim = NULL, mlim = NULL, rounded = TRUE)

```

Arguments

cost.model	logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned object from function od.1 ; default value is NULL; if expr is specified, parameter values of r12, c1, c1t, and p used or solved in function od.1 will be passed to the current function; only the value of p that specified or solved in function od.1 can be overwritten if constraint is specified.
constraint	specify the constrained value of p in list format to overwrite that from expr; default value is NULL.
sig.level	significance level or type I error rate, default value is 0.05.
two.tailed	logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	effect size.
power	statistical power.
m	total budget.
n	the total sample size.

p	the proportion of individuals to be assigned to treatment.
r12	the proportion of outcome variance explained by covariates.
q	the number of covariates.
c1	the cost of sampling one unit in control condition.
c1t	the cost of sampling one unit in treatment condition.
dlim	the range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	the range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
nlim	the range for searching the root of sample size (n) numerically, default value is c(4, 10e10)
mlim	the range for searching the root of budget (m) numerically, default value is the costs sampling nlim units across treatment conditions or c(4 * ncost, 10e10 * ncost) with ncost = ((1 - p) * c1 + p * c1t)
rounded	logical; round p that is from functions od.1 to two decimal places if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (or required sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design
myod1 <- od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2))
myod1$out # p = 0.31

# ----- power analyses by default considering costs and budget -----
# required budget and sample size
mym.1 <- power.1(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 1032 n = 461
# mym.1$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
mym.1 <- power.1(d = 0.2, power = 0.8, c1 = 1, c1t = 5,
  r12 = 0.5, p = 0.31, q = 1)
# required budget and sample size with constrained p
mym.2 <- power.1(expr = myod1, d = 0.2, q = 1, power = 0.8,
  constraint = list(p = 0.5))
mym.2$out # m = 1183, n = 394
```

```

# Power calculation
mypower <- power.1(expr = myod1, q = 1, d = 0.2, m = 1032)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.1(expr = myod1, q = 1, d = 0.2, m = 1032,
  constraint = list(p = 0.5))
mypower.1$out # power = 0.74

# MDES calculation
mymdes <- power.1(expr = myod1, q = 1, power = 0.80, m = 1032)
mymdes$out # d = 0.20

# ----- conventional power analyses with cost.model = FALSE-----
# Required sample size n
myn <- power.1(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myn$out # n = 461
# myn$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
myn <- power.1(cost.model = FALSE, d = 0.2, power = 0.8,
  r12 = 0.5, p = 0.31, q = 1)

# Power calculation
mypower1 <- power.1(cost.model = FALSE, expr = myod1, n = 461, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.1(cost.model = FALSE, expr = myod1, n = 461, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

power.2 *Budget and/or sample size, power, MDES calculation for two-level CRTs*

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for two-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.2(cost.model = TRUE, expr = NULL, constraint = NULL,
  sig.level = 0.05, two.tailed = TRUE, d = NULL, power = NULL,
  m = NULL, n = NULL, J = NULL, p = NULL, icc = NULL,
  r12 = NULL, r22 = NULL, q = NULL, c1 = NULL, c2 = NULL,
  c1t = NULL, c2t = NULL, dlim = NULL, powerlim = NULL,
  Jlim = NULL, mlim = NULL, rounded = TRUE)

```

Arguments

cost.model	logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned object from function <code>od.2</code> ; default is NULL; if <code>expr</code> is specified, parameter values of <code>icc</code> , <code>r12</code> , <code>r22</code> , <code>c1</code> , <code>c2</code> , <code>c1t</code> , <code>c2t</code> , <code>n</code> , and <code>p</code> used or solved in function <code>od.2</code> will be passed to the current function; only the values of <code>n</code> and <code>p</code> that specified or solved in function <code>od.2</code> can be overwritten if <code>constraint</code> is specified.
constraint	specify the constrained values of <code>n</code> and/or <code>p</code> in list format to overwrite those from <code>expr</code> ; default is NULL.
sig.level	significance level or type I error rate, default value is 0.05.
two.tailed	logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	effect size.
power	statistical power.
m	total budget.
n	the level-1 sample size per level-2 unit.
J	the total level-2 sample size.
p	the proportion of level-2 clusters/units to be assigned to treatment.
icc	the unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	the proportion of level-1 variance explained by covariates.
r22	the proportion of level-2 variance explained by covariates.
q	the number of level-2 covariates.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
dlim	the range for searching the root of effect size (<code>d</code>) numerically, default value is <code>c(0, 5)</code> .
powerlim	the range for searching the root of power (<code>power</code>) numerically, default value is <code>c(1e-10, 1 - 1e-10)</code> .
Jlim	the range for searching the root of level-2 sample size (<code>J</code>) numerically, default is <code>c(4, 10e10)</code>
mlim	the range for searching the root of budget (<code>m</code>) numerically, default is the costs sampling <code>Jlim</code> level-2 units across treatment conditions or <code>c(4 * Jcost, 10e10 * Jcost)</code> , with $Jcost = ((1 - p) * (c1 * n + c2) + p * (c1t * n + c2t))$
rounded	logical; round <code>n</code> and <code>p</code> that are from functions <code>od.2</code> to integer and two decimal places, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-2 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2018, April). Optimal design of cluster randomized trials under condition- and unit-specific cost structures. Roundtable discussion presented at American Educational Research Association (AERA) annual conference, New York City, NY;

Shen, Z., & Kelcey, B. (revise & resubmit). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*.

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50)
myod1$out # n = 8.9, p = 0.33

# ----- power analyses by default considering costs and budget -----
# required budget and sample size
mym.1 <- power.2(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 3755, J = 130.2
#mym.1$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
mym.1 <- power.2(d = 0.2, power = 0.8, icc = 0.2,
                 c1 = 1, c2 = 5, c1t = 1, c2t = 50,
                 r12 = 0.5, r22 = 0.5, n = 9, p = 0.33, q = 1)
# required budget and sample size with constrained p
mym.2 <- power.2(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 4210, J = 115.3
# required budget and sample size with constrained p and n
mym.3 <- power.2(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 20))
mym.3$out # m = 4568, J = 96.2

# Power calculation
mypower <- power.2(expr = myod1, q = 1, d = 0.2, m = 3755)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.2(expr = myod1, q = 1, d = 0.2, m = 3755,
                    constraint = list(p = 0.5))
mypower.1$out # power = 0.75

# MDES calculation
mymdes <- power.2(expr = myod1, q = 1, power = 0.80, m = 3755)
```

```

mymdes$out # d = 0.20

# ----- conventional power analyses with cost.model = FALSE-----
# Required J
myJ <- power.2(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myJ$out # J = 130.2
#myJ$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
myJ <- power.2(cost.model = FALSE, d = 0.2, power = 0.8, icc = 0.2,
               r12 = 0.5, r22 = 0.5, n = 9, p = 0.33, q = 1)

# Power calculation
mypower1 <- power.2(cost.model = FALSE, expr = myod1, J = 130, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.2(cost.model = FALSE, expr = myod1, J = 130, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

power.2m

*Budget and/or sample size, power, MDES calculation for two-level
multisite randomized trials*

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for two-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.2m(cost.model = TRUE, expr = NULL, constraint = NULL,
         sig.level = 0.05, two.tailed = TRUE, d = NULL, power = NULL,
         m = NULL, n = NULL, J = NULL, p = NULL, icc = NULL,
         r12 = NULL, r22m = NULL, q1 = NULL, q2 = NULL, c1 = NULL,
         c2 = NULL, c1t = NULL, omega = NULL, dlim = NULL,
         powerlim = NULL, Jlim = NULL, mlim = NULL, rounded = TRUE)

```

Arguments

cost.model	logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned objects from function od.2m ; default is NULL; if expr is specified, parameter values of icc, r12, r22m, c1, c2, c1t, p, and n used or solved in function od.2m will be passed to current function; only the values of p and n

	that specified or solved in function od.2m can be overwritten if constraint is specified.
constraint	specify the constrained values of p and/or n in list format to overwrite those from expr; default value is NULL.
sig.level	significance level or type I error rate, default value is 0.05.
two.tailed	logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	effect size.
power	statistical power.
m	total budget.
n	the level-1 sample size per level-2 unit.
J	the level-2 sample size per level-3 unit.
p	the proportion of level-1 units to be assigned to treatment.
icc	the unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	the proportion of level-1 variance explained by covariates.
r22m	the proportion of variance of site-specific treatment effect explained by covariates.
q1	the number of covariates at level 1.
q2	the number of covariates at level 2.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit.
c1t	the cost of sampling one level-1 unit in treatment condition.
omega	the standardized variance of site-specific treatment effect
dlim	the range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	the range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
Jlim	the range for searching the root of level-2 sample size (J) numerically, default is c(4, 10e10)
m1im	the range for searching the root of budget (m) numerically, default is the costs sampling Jlim level-2 units or c(4 * Jcost, 1e+10 * Jcost) with Jcost = (1 - p) * c1 * n + p * c1t * n + c2.
rounded	logical; round the values of p, n/J/K that are from functions od.4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-2 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.2m(icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005))
myod1$out # n = 20, p = 0.37

# ----- power analyses by default considering costs and budget -----
# required budget and sample size
mym.1 <- power.2m(expr = myod1, d = 0.2, q1 = 1, q2 = 1, power = 0.8)
mym.1$out # m = 612, J = 6.3
# mym.1$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
mym.1 <- power.2m(d = 0.2, power = 0.8, q1 = 1, q2 = 1,
                 icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
                 c1 = 1, c2 = 10, c1t = 10,
                 n = 20, p = 0.37)
# required budget and sample size with constrained p
mym.2 <- power.2m(expr = myod1, d = 0.2, q1 = 1, q2 = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 726, J = 6.1
# required budget and sample size with constrained p and n
mym.3 <- power.2m(expr = myod1, d = 0.2, q1 = 1, q2 = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 5))
mym.3$out # m = 702, J = 18.7

# Power calculation
mypower <- power.2m(expr = myod1, q1 = 1, q2 = 1, d = 0.2, m = 612)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.2m(expr = myod1, q1 = 1, q2 = 1, d = 0.2, m = 612,
                    constraint = list(p = 0.5))
mypower.1$out # power = 0.73

# MDES calculation
mymdes <- power.2m(expr = myod1, q1 = 1, q2 = 1, power = 0.80, m = 612)
mymdes$out # d = 0.20

# ----- conventional power analyses with cost.model = FALSE-----
# Required sample size
myJ <- power.2m(cost.model = FALSE, expr = myod1, d = 0.2, q1 = 1, q2 = 1, power = 0.8)
myJ$out # J = 6.3
# myL$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
myJ <- power.2m(cost.model = FALSE, d = 0.2, power = 0.8, q1 = 1, q2 = 1,
```

```

      icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
      c1 = 1, c2 = 10, c1t = 10,
      n = 20, p = 0.37)

# Power calculation
mypower1 <- power.2m(cost.model = FALSE, expr = myod1, J = 6.3, d = 0.2, q1 = 1, q2 = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.2m(cost.model = FALSE, expr = myod1, J = 6.3, power = 0.8, q1 = 1, q2 = 1)
mymdes1$out # d = 0.20

```

power.3	<i>Budget and/or sample size, power, MDES calculation for three-level CRTs</i>
---------	--

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for three-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.3(cost.model = TRUE, expr = NULL, constraint = NULL,
  sig.level = 0.05, two.tailed = TRUE, d = NULL, power = NULL,
  m = NULL, n = NULL, J = NULL, K = NULL, p = NULL,
  icc2 = NULL, icc3 = NULL, r12 = NULL, r22 = NULL, r32 = NULL,
  q = NULL, c1 = NULL, c2 = NULL, c3 = NULL, c1t = NULL,
  c2t = NULL, c3t = NULL, dlim = NULL, powerlim = NULL,
  Klim = NULL, mlim = NULL, rounded = TRUE)

```

Arguments

cost.model	logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned objects from function od.3 ; default is NULL; if expr is specified, parameter values of icc2, icc3, r12, r22, r32, c1, c2, c3, c1t, c2t, c3t, p, n, and J used or solved in function od.3 will be passed to the current function; only the values of p, n, and/or J that specified or solved in function od.3 can be overwritten if constraint is specified.
constraint	specify the constrained values of p, n, and/or J in list format to overwrite those from expr; default is NULL.
sig.level	significance level or type I error rate, default value is 0.05.

two.tailed	logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	effect size.
power	statistical power.
m	total budget.
n	the level-1 sample size per level-2 unit.
J	the level-2 sample size per level-3 unit.
K	the total level-3 sample size.
p	the proportion of level-3 clusters/units assigned to treatment.
icc2	the unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	the unconditional intraclass correlation coefficient (ICC) at level 3.
r12	the proportion of level-1 variance explained by covariates.
r22	the proportion of level-2 variance explained by covariates.
r32	the proportion of level-3 variance explained by covariates.
q	the number of covariates at level 3.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c3	the cost of sampling one level-3 unit in control condition.
c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
c3t	the cost of sampling one level-3 unit in treatment condition.
dlim	the range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	the range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
Klim	the range for searching the root of level-3 sample size (K) numerically, default value is c(4, 1e+10)
mlim	the range for searching the root of budget (m) numerically, default value is the costs sampling Klim level-3 units across treatment conditions or $c(4 * Kcost, 1e+10 * Kcost)$ with $Kcost = ((1 - p) * (c1 * n * J + c2 * J + c3) + p * (c1t * n * J + c2t * J + c3t))$
rounded	logical; round the values of p, n/J that are from functions od.3 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-3 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (revise & resubmit). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*.

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250)
myod1$out # output # n = 7.9, J = 3.2, p = 0.28

# ----- power analyses by default considering costs and budget -----
# required budget and sample size
mym.1 <- power.3(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 16032, K = 97.3
#mym.1$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
mym.1 <- power.3(d = 0.2, power = 0.8, q = 1,
                 icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
                 c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
                 n = 8, J = 3, p = 0.28)
# required budget and sample size with constrained p
mym.2 <- power.3(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 19239, K = 78.8
# required budget and sample size with constrained p and J
mym.3 <- power.3(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, J = 20))
mym.3$out # m = 39774, K = 46.9

# Power calculation
mypower <- power.3(expr = myod1, q = 1, d = 0.2, m = 16032)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.3(expr = myod1, q = 1, d = 0.2, m = 16032,
                     constraint = list(p = 0.5))
mypower.1$out # power = 0.72

# MDES calculation
mymdes <- power.3(expr = myod1, q = 1, power = 0.80, m = 16032)
mymdes$out # d = 0.20

# ----- conventional power analyses with cost.model = FALSE-----
# Required sample size
myK <- power.3(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myK$out # K = 97.3
#myK$par # parameters and their values used for the function
```

```
# or equivalently, specify every argument in the function
myK <- power.3(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
              icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
              n = 8, J = 3, p = 0.28)

# Power calculation
mypower1 <- power.3(cost.model = FALSE, expr = myod1, K = 97, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.3(cost.model = FALSE, expr = myod1, K = 97, power = 0.8, q = 1)
mymdes1$out # d = 0.20
```

power.3m

Budget and/or sample size, power, MDES calculation for three-level multisite randomized trials

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for three-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.3m(cost.model = TRUE, expr = NULL, constraint = NULL,
         sig.level = 0.05, two.tailed = TRUE, d = NULL, power = NULL,
         m = NULL, n = NULL, J = NULL, K = NULL, p = NULL,
         icc2 = NULL, icc3 = NULL, r12 = NULL, r22 = NULL, r32m = NULL,
         q2 = NULL, q3 = NULL, c1 = NULL, c2 = NULL, c3 = NULL,
         c1t = NULL, c2t = NULL, omega = NULL, dlim = NULL,
         powerlim = NULL, Klim = NULL, mlim = NULL, rounded = TRUE)
```

Arguments

cost.model	logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned objects from function od.3m ; default is NULL; if expr is specified, parameter values of icc2, icc3, r12, r22, r32m, c1, c2, c3, c1t, c2t, p, n, and J used or solved in function od.3m will be passed to current function; only the values of p, n, and/or J that specified or solved in function od.3m can be overwritten if constraint is specified.
constraint	specify the constrained values of p, n, and/or J, in list format to overwrite those from expr; default value is NULL.

sig.level	significance level or type I error rate, default value is 0.05.
two.tailed	logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	effect size.
power	statistical power.
m	total budget.
n	the level-1 sample size per level-2 unit.
J	the level-2 sample size per level-3 unit.
K	the level-3 sample size per level-4 unit.
p	the proportion of level-2 units to be assigned to treatment.
icc2	the unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	the unconditional intraclass correlation coefficient (ICC) at level 3.
r12	the proportion of level-1 variance explained by covariates.
r22	the proportion of level-2 variance explained by covariates.
r32m	the proportion of variance of site-specific treatment effect explained by covariates.
q2	the number of covariates at level 2.
q3	the number of covariates at level 3.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c3	the cost of sampling one level-3 unit.
c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
omega	the standardized variance of site-specific treatment effect
dlim	the range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	the range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
Klim	the range for searching the root of level-3 sample size (K) numerically, default value is c(4, 1e+10)
m1im	the range for searching the root of budget (m) numerically, default is the costs sampling Klim level-3 units or c(4 * Kcost, 1e+10 * Kcost) with Kcost = ((1 - p) * (c1 * n * J + c2 * J) + p * (c1t * n * J + c2t * J) + c3.
rounded	logical; round the values of p, n/J/K that are from functions od. 4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-3 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005))
myod1$out # n = 13, J = 15, p = 0.23

# ----- power analyses by default considering costs and budget -----
# required budget and sample size
mym.1 <- power.3m(expr = myod1, d = 0.2, q2 = 1, q3 = 1, power = 0.8)
mym.1$out # m = 13177, K = 11.5
# mym.1$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
mym.1 <- power.3m(d = 0.2, power = 0.8, q2 = 1, q3 = 1,
                 icc2 = 0.2, icc3 = 0.1, omega = 0.02,
                 r12 = 0.5, r22 = 0.5, r32m = 0.5,
                 c1 = 1, c2 = 5,
                 c1t = 1, c2t = 200, c3 = 200,
                 n = 13, J = 15, p = 0.23)
# required budget and sample size with constrained p
mym.2 <- power.3m(expr = myod1, d = 0.2, q2 = 1, q3 = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 17026, K = 8.8
# required budget and sample size with constrained p and n
mym.3 <- power.3m(expr = myod1, d = 0.2, q2 = 1, q3 = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 20))
mym.3$out # m = 16954, K = 8.3

# Power calculation
mypower <- power.3m(expr = myod1, q2 = 1, q3 = 1, d = 0.2, m = 13177)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.3m(expr = myod1, q2 = 1, q3 = 1, d = 0.2, m = 13177,
                    constraint = list(p = 0.5))
mypower.1$out # power = 0.69

# MDES calculation
mymdes <- power.3m(expr = myod1, q2 = 1, q3 = 1, power = 0.80, m = 13176)
mymdes$out # d = 0.20

# ----- conventional power analyses with cost.model = FALSE-----
# Required sample size
myK <- power.3m(cost.model = FALSE, expr = myod1, d = 0.2, q2 = 1, q3 = 1, power = 0.8)
```



```

myK$out # K = 11.5
# myK$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
myK <- power.3m(cost.model = FALSE, d = 0.2, power = 0.8, q2 = 1, q3 = 1,
               icc2 = 0.2, icc3 = 0.1, omega = 0.02,
               r12 = 0.5, r22 = 0.5, r32m = 0.5,
               c1 = 1, c2 = 5,
               c1t = 1, c2t = 200, c3 = 200,
               n = 13, J = 15, p = 0.23)

# Power calculation
mypower1 <- power.3m(cost.model = FALSE, expr = myod1, K = 11.5, d = 0.2, q2 = 1, q3 = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.3m(cost.model = FALSE, expr = myod1, K = 11.5, power = 0.8, q2 = 1, q3 = 1)
mymdes1$out # d = 0.20

```

power.4

Budget and/or sample size, power, MDES calculation for four-level CRTs

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for four-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.4(cost.model = TRUE, expr = NULL, constraint = NULL,
        sig.level = 0.05, two.tailed = TRUE, d = NULL, power = NULL,
        m = NULL, n = NULL, J = NULL, K = NULL, L = NULL, p = NULL,
        icc2 = NULL, icc3 = NULL, icc4 = NULL, r12 = NULL, r22 = NULL,
        r32 = NULL, r42 = NULL, q = NULL, c1 = NULL, c2 = NULL,
        c3 = NULL, c4 = NULL, c1t = NULL, c2t = NULL, c3t = NULL,
        c4t = NULL, dlim = NULL, powerlim = NULL, Llim = NULL,
        mlim = NULL, rounded = TRUE)

```

Arguments

cost.model	logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned objects from function od.4 ; default value is NULL; if expr is specified, parameter values of icc2, icc3, icc4, r12, r22, r32, r42, c1, c2, c3, c4, c1t,

c2t, c3t, c4t, p, n, J, and K used or solved in function [od.4](#) will be passed to current function; only the values of p, n, J, and/or K that specified or solved in function [od.4](#) can be overwritten if constraint is specified.

constraint	specify the constrained values of p, n, J, and/or K in list format to overwrite those from expr; default value is NULL.
sig.level	significance level or type I error rate, default value is 0.05.
two.tailed	logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	effect size.
power	statistical power.
m	total budget.
n	the level-1 sample size per level-2 unit.
J	the level-2 sample size per level-3 unit.
K	the level-3 sample size per level-4 unit.
L	the total level-4 sample size.
p	the proportion of level-4 clusters/units to be assigned to treatment.
icc2	the unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	the unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	the unconditional intraclass correlation coefficient (ICC) at level 4.
r12	the proportion of level-1 variance explained by covariates.
r22	the proportion of level-2 variance explained by covariates.
r32	the proportion of level-3 variance explained by covariates.
r42	the proportion of level-4 variance explained by covariates.
q	the number of covariates at level 4.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c3	the cost of sampling one level-3 unit in control condition.
c4	the cost of sampling one level-4 unit in control condition.
c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
c3t	the cost of sampling one level-3 unit in treatment condition.
c4t	the cost of sampling one level-4 unit in treatment condition.
dlim	the range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	the range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
Llim	the range for searching the root of level-4 sample size (L) numerically, default value is c(4, 1e+10).

mLim	the range for searching the root of budget (m) numerically, default value is the costs sampling LLim level-4 units across treatment conditions or $c(4 * Lcost, 1e+10 * Lcost)$ with $Lcost = ((1 - p) * (c1 * n * J * K + c2 * J * K + c3 * K + c4) + p * (c1t * n * J * K + c2t * J * K + c3t * K + c4t))$.
rounded	logical; round the values of p, n/J/K that are from functions od.4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-4 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500)
myod1$out # output # n = 7.1, J = 3.2, K = 4.2, p = 0.23

# ----- power analyses by default considering costs and budget -----
# required budget and sample size
mym.1 <- power.4(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 71161, L = 57.1
#mym.1$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
mym.1 <- power.4(d = 0.2, power = 0.8, q = 1,
                icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
                r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
                c1 = 1, c2 = 5, c3 = 25, c4 = 125,
                c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
                n = 7, J = 3, K = 4, p = 0.23)
# required budget and sample size with constrained p (p = 0.5)
mym.2 <- power.4(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 93508, L = 41.1
# required budget and sample size with constrained p and K
mym.3 <- power.4(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, K = 20))
mym.3$out # m = 157365, L = 25.7

# Power calculation
```

```

mypower <- power.4(expr = myod1, q = 1, d = 0.2, m = 71161)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.4(expr = myod1, q = 1, d = 0.2, m = 71161,
  constraint = list(p = 0.5))
mypower.1$out # power = 0.68

# MDES calculation
mymdes <- power.4(expr = myod1, q = 1, power = 0.80, m = 71161)
mymdes$out # d = 0.20

# ----- conventional power analyses with cost.model = FALSE-----
# Required sample size
myL <- power.4(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myL$out # L = 57.1
#myL$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
myL <- power.4(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
  icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
  r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
  n = 7, J = 3, K = 4, p = 0.23)

# Power calculation
mypower1 <- power.4(cost.model = FALSE, expr = myod1, L = 57, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.4(cost.model = FALSE, expr = myod1, L = 57, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

power.4m

*Budget and/or sample size, power, MDES calculation for four-level
multisite randomized trials*

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for four-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.4m(cost.model = TRUE, expr = NULL, constraint = NULL,
  sig.level = 0.05, two.tailed = TRUE, d = NULL, power = NULL,
  m = NULL, n = NULL, J = NULL, K = NULL, L = NULL, p = NULL,
  icc2 = NULL, icc3 = NULL, icc4 = NULL, r12 = NULL, r22 = NULL,
  r32 = NULL, r42m = NULL, q3 = NULL, q4 = NULL, c1 = NULL,
  c2 = NULL, c3 = NULL, c4 = NULL, c1t = NULL, c2t = NULL,

```

c3t = NULL, omega = NULL, dlim = NULL, powerlim = NULL,
l1lim = NULL, mlim = NULL, rounded = TRUE)

Arguments

cost.model	logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned objects from function od.4m ; default is NULL; if expr is specified, parameter values of icc2, icc3, icc4, r12, r22, r32, r42m, c1, c2, c3, c4, c1t, c2t, c3t, p, n, J, and K used or solved in function od.4m will be passed to current function; only the values of p, n, J, and/or K that specified or solved in function od.4m can be overwritten if constraint is specified.
constraint	specify the constrained values of p, n, J, and/or K in list format to overwrite those from expr; default value is NULL.
sig.level	significance level or type I error rate, default value is 0.05.
two.tailed	logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	effect size.
power	statistical power.
m	total budget.
n	the level-1 sample size per level-2 unit.
J	the level-2 sample size per level-3 unit.
K	the level-3 sample size per level-4 unit.
L	the total level-4 sample size.
p	the proportion of level-3 units to be assigned to treatment.
icc2	the unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	the unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	the unconditional intraclass correlation coefficient (ICC) at level 4.
r12	the proportion of level-1 variance explained by covariates.
r22	the proportion of level-2 variance explained by covariates.
r32	the proportion of level-3 variance explained by covariates.
r42m	the proportion of variance of site-specific treatment effect explained by covariates.
q3	the number of covariates at level 3.
q4	the number of covariates at level 4.
c1	the cost of sampling one level-1 unit in control condition.
c2	the cost of sampling one level-2 unit in control condition.
c3	the cost of sampling one level-3 unit in control condition.
c4	the cost of sampling one level-4 unit.

c1t	the cost of sampling one level-1 unit in treatment condition.
c2t	the cost of sampling one level-2 unit in treatment condition.
c3t	the cost of sampling one level-3 unit in treatment condition.
omega	the standardized variance of site-specific treatment effect
dlim	the range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	the range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
Llim	the range for searching the root of level-4 sample size (L) numerically, default value is c(4, 1e+10).
mlim	the range for searching the root of budget (m) numerically, default is the costs sampling Llim level-4 units or $c(4 * Lcost, 1e+10 * Lcost)$ with $Lcost = ((1 - p) * (c1 * n * J * K + c2 * J * K + c3 * K) + p * (c1t * n * J * K + c2t * J * K + c3t * K) + c4$.
rounded	logical; round the values of p, n/J/K that are from functions od.4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-4 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design #-----
myod1 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
             c1t = 1, c2t = 50, c3t = 250, c4 = 500,
             varlim = c(0, 0.005))
myod1$out # n = 8.3, J = 3.2, K = 4.9, p = 0.36

# ----- power analyses by default considering costs and budget -----
# required budget and sample size
mym.1 <- power.4m(expr = myod1, d = 0.2, q3 = 1, q4 = 1, power = 0.8)
mym.1$out # m = 28668, L = 19.5
# mym.1$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
mym.1 <- power.4m(d = 0.2, power = 0.8, q3 = 1, q4 = 1,
                 icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
```

```

        r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
        c1 = 1, c2 = 5, c3 = 25,
        c1t = 1, c2t = 50, c3t = 250, c4 = 500,
        n = 8, J = 3, K = 5, p = 0.36)
# required budget and sample size with constrained p
mym.2 <- power.4m(expr = myod1, d = 0.2, q3 = 1, q4 = 1, power = 0.8,
  constraint = list(p = 0.5))
mym.2$out # m = 31379, L = 18.2
# required budget and sample size with constrained p and n
mym.3 <- power.4m(expr = myod1, d = 0.2, q3 = 1, q4 = 1, power = 0.8,
  constraint = list(p = 0.5, n = 20))
mym.3$out # m = 32257, L = 17.0

# Power calculation
mypower <- power.4m(expr = myod1, q3 = 1, q4 = 1, d = 0.2, m = 28668)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.4m(expr = myod1, q3 = 1, q4 = 1, d = 0.2, m = 28668,
  constraint = list(p = 0.5))
mypower.1$out # power = 0.76

# MDES calculation
mymdes <- power.4m(expr = myod1, q3 = 1, q4 = 1, power = 0.80, m = 28668)
mymdes$out # d = 0.20

# ----- conventional power analyses with cost.model = FALSE-----
# Required sample size
myL <- power.4m(cost.model = FALSE, expr = myod1, d = 0.2, q3 = 1, q4 = 1, power = 0.8)
myL$out # L = 19.5
# myL$par # parameters and their values used for the function
# or equivalently, specify every argument in the function
myL <- power.4m(cost.model = FALSE, d = 0.2, power = 0.8, q3 = 1, q4 = 1,
  icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
  r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
  c1 = 1, c2 = 5, c3 = 25,
  c1t = 1, c2t = 50, c3t = 250, c4 = 500,
  n = 8, J = 3, K = 5, p = 0.36)

# Power calculation
mypower1 <- power.4m(cost.model = FALSE, expr = myod1, L = 19.5, d = 0.2, q3 = 1, q4 = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.4m(cost.model = FALSE, expr = myod1, L = 19.5, power = 0.8, q3 = 1, q4 = 1)
mymdes1$out # d = 0.20

```

Description

Calculate the relative efficiency (RE) between two designs, it returns same results as those from function [rpe](#)

Usage

```
re(od, subod, rounded = TRUE, verbose = TRUE)
```

Arguments

od	returned object of first design (e.g., unconstrained optimal design) from function od.1 , od.2 , od.3 , od.4 , od.2m , od.3m , or od.4m
subod	returned object of second design (e.g., constrained optimal design) from function od.1 , od.2 , od.3 , od.4 , od.2m , od.3m , or od.4m
rounded	logical; round the values of p , $n/J/K$ that are from functions to two decimal places and integer, respectively if TRUE, no rounding if FALSE; default is TRUE.
verbose	logical; print the value of relative efficiency if TRUE, otherwise not; default is TRUE.

Value

Relative efficiency value

References

Shen, Z., & Kelcey, B. (2018, April). Optimal design of cluster randomized trials under condition- and unit-specific cost structures. Roundtable discussion presented at American Educational Research Association (AERA) annual conference, New York City, NY;

Shen, Z., & Kelcey, B. (revise & resubmit). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*.

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design of 2-level CRT #-----
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             varlim = c(0.01, 0.02))
# constrained optimal design with n = 20
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             n = 20, varlim = c(0.005, 0.025))
# relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$out # RE = 0.88
# constrained optimal design with p = 0.5
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             p = 0.5, varlim = c(0.005, 0.025))
# relative efficiency (RE)
```



```

myre <- re(od = myod1, subod= myod2)
myre$out # RE = 0.90

# unconstrained optimal design of 3-level CRT #-----
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
# constrained optimal design with J = 20
myod2 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$out # RE = 0.53

# unconstrained optimal design of 4-level CRT #-----
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
# constrained optimal design with p = 0.5
myod2 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5, p = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
# relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$out # RE = 0.78

```

rpe

Relative precision and efficiency (RPE) calculation

Description

Calculate the relative precision and efficiency (RPE) between two designs, it returns same results as those from function [re](#)

Usage

```
rpe(od, subod, rounded = TRUE, verbose = TRUE)
```

Arguments

od	returned object of first design (e.g., unconstrained optimal design) from function od.1 , od.2 , od.3 , od.4 , od.2m , od.3m , or od.4m
subod	returned object of second design (e.g., constrained optimal design) from function od.1 , od.2 , od.3 , od.4 , od.2m , od.3m , or od.4m

rounded	logical; round the values of p , $n/J/K$ that are from functions to two decimal places and integer, respectively if TRUE, no rounding if FALSE; default is TRUE.
verbose	logical; print the value of relative precision and efficiency if TRUE, otherwise not; default is TRUE.

Value

Relative precision and efficiency value.

References

Shen, Z., & Kelcey, B. (2018, April). Optimal design of cluster randomized trials under condition- and unit-specific cost structures. Roundtable discussion presented at American Educational Research Association (AERA) annual conference, New York City, NY;

Shen, Z., & Kelcey, B. (revise & resubmit). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*.

Shen, Z. (in progress). Using optimal sample allocation to improve statistical precision and design efficiency for multilevel randomized trials (Unpublished doctoral dissertation). University of Cincinnati, Cincinnati, OH.

Examples

```
# unconstrained optimal design of 2-level CRT #-----
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             varlim = c(0.01, 0.02))
# constrained optimal design with n = 20
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             n = 20, varlim = c(0.005, 0.025))
# relative precision and efficiency (RPE)
myrpe <- rpe(od = myod1, subod= myod2)
myrpe$out # RPE = 0.88
# constrained optimal design with p = 0.5
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             p = 0.5, varlim = c(0.005, 0.025))
# relative precision and efficiency (RPE)
mypre <- rpe(od = myod1, subod= myod2)
mypre$out # RPE = 0.90

# unconstrained optimal design of 3-level CRT #-----
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
# constrained optimal design with J = 20
myod2 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
# relative precision and efficiency (RPE)
myrpe <- rpe(od = myod1, subod= myod2)
myrpe$out # RPE = 0.53

# unconstrained optimal design of 4-level CRT #-----
```

```
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
# constrained optimal design with p = 0.5
myod2 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5, p = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
# relative precision and efficiency (RPE)
myrpe <- rpe(od = myod1, subod = myod2)
myrpe$out # RPE = 0.78
```

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