

# Package ‘CARBayesST’

January 8, 2019

**Type** Package

**Title** Spatio-Temporal Generalised Linear Mixed Models for Areal Unit Data

**Version** 3.0.1

**Date** 2019-01-03

**Author** Duncan Lee, Alastair Rushworth and Gary Napier

**Maintainer** Duncan Lee <Duncan.Lee@glasgow.ac.uk>

## Description

Implements a class of spatio-temporal generalised linear mixed models for areal unit data, with inference in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation. The response variable can be binomial, Gaussian, or Poisson, but for some models only the binomial and Poisson data likelihoods are available. The spatio-temporal autocorrelation is modelled by random effects, which are assigned conditional autoregressive (CAR) style prior distributions. A number of different random effects structures are available, including Bernardinelli et al. (1995) <doi:10.1002/sim.4780142112>, Rushworth et al. (2014) <doi:10.1016/j.sste.2014.05.001> and Lee et al. (2016) <doi:10.1214/16-AOAS941>. Full details are given in the vignette accompanying this package. The creation of this package was supported by the Engineering and Physical Sciences Research Council (EPSRC) grant EP/J017442/1 and the Medical Research Council (MRC) grant MR/L022184/1.

**License** GPL (>= 2)

**Depends** MASS, R (>= 3.0.0), Rcpp (>= 0.11.5)

**Imports** CARBayesdata, coda, dplyr, gtools, leaflet, matrixcalc, matrixStats, rgdal, sp, spam, spdep, stats, testthat, truncdist, truncnorm, utils

**LinkingTo** Rcpp

**LazyLoad** yes

**ByteCompile** yes

**URL** <http://github.com/duncanplee/CARBayesST>

**BugReports** <http://github.com/duncanplee/CARBayesST/issues>

**NeedsCompilation** yes

**Repository** CRAN

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## R topics documented:

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CARBayesST-package	<i>Spatio-Temporal Generalised Linear Mixed Models For Areal Unit Data</i>
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## Description

Implements a class of spatio-temporal generalised linear mixed models for areal unit data, with inference in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation. The response variable can be binomial, Gaussian or Poisson, but for some models only the binomial and Poisson data likelihoods are available. The spatio-temporal autocorrelation is modelled by random effects, which are assigned conditional autoregressive (CAR) style prior distributions. A number of different random effects structures are available, and full details are given in the vignette accompanying this package and the references below. The creation of this package was supported by the Engineering and Physical Sciences Research Council (EPSRC) grant EP/J017442/1 and the Medical Research Council (MRC) grant MR/L022184/1.

## Details

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**Author(s)**

Author: Duncan Lee, Alastair Rushworth and Gary Napier

Maintainer: Duncan Lee <Duncan.Lee@glasgow.ac.uk>

**References**

Bernardinelli, L., D. Clayton, C.Pascuto, C.Montomoli, M.Ghislandi, and M. Songini (1995). Bayesian analysis of space-time variation in disease risk. *Statistics in Medicine*, 14, 2433-2443.

Knorr-Held, L. (2000). Bayesian modelling of inseparable space-time variation in disease risk. *Statistics in Medicine*, 19, 2555-2567.

Lee, D and Lawson, C (2016). Quantifying the spatial inequality and temporal trends in maternal smoking rates in Glasgow, *Annals of Applied Statistics*, 10, 1427-1446.

Lee, D and Rushworth, A and Napier, G (2018). Spatio-Temporal Areal Unit Modeling in R with Conditional Autoregressive Priors Using the CARBayesST Package, *Journal of Statistical Software*, 84, 9, 1-39.

Napier, G, D. Lee, C. Robertson, A. Lawson, and K. Pollock (2016). A model to estimate the impact of changes in MMR vaccination uptake on inequalities in measles susceptibility in Scotland, *Statistical Methods in Medical Research*, 25, 1185-1200.

Rushworth, A., D. Lee, and R. Mitchell (2014). A spatio-temporal model for estimating the long-term effects of air pollution on respiratory hospital admissions in Greater London. *Spatial and Spatio-temporal Epidemiology* 10, 29-38.

Rushworth, A., Lee, D., and Sarran, C (2017). An adaptive spatio-temporal smoothing model for estimating trends and step changes in disease risk. *Journal of the Royal Statistical Society Series C*, 66, 141-157.

**Examples**

```
## See the examples in the function specific help files and in the vignette
## accompanying this package.
```

---

```
coef.CARBayesST      Extract the regression coefficients from a model.
```

---

**Description**

This function takes a CARBayesST object and returns the vector of estimated regression coefficients (posterior medians).

**Usage**

```
## S3 method for class 'CARBayesST'
coef(object, ...)
```

**Arguments**

object            A CARBayesST fitted model object.  
 ...              Ignored.

**Author(s)**

Duncan Lee

---

fitted.CARBayesST      *Extract the fitted values from a model.*

---

**Description**

This function takes a CARBayesST object and returns the vector of fitted values (posterior means).

**Usage**

```
## S3 method for class 'CARBayesST'
fitted(object, ...)
```

**Arguments**

object            A CARBayesST fitted model object.  
 ...              Ignored.

**Author(s)**

Duncan Lee

---

logLik.CARBayesST      *Extract the estimated loglikelihood from a fitted model.*

---

**Description**

This function takes a CARBayesST object and returns the estimated loglikelihood (posterior means).

**Usage**

```
## S3 method for class 'CARBayesST'
logLik(object, ...)
```

**Arguments**

object            A CARBayesST fitted model object.  
 ...              Ignored.

**Author(s)**

Duncan Lee

---

`model.matrix.CARBayesST`*Extract the model (design) matrix from a model.*

---

**Description**

This function takes a CARBayesST object and returns the design matrix.

**Usage**

```
## S3 method for class 'CARBayesST'  
model.matrix(object, ...)
```

**Arguments**

<code>object</code>	A CARBayesST fitted model object.
<code>...</code>	Ignored.

**Author(s)**

Duncan Lee

---

`print.CARBayesST`*Print a summary of the fitted model to the screen.*

---

**Description**

This function takes a CARBayesST object and returns a summary of the fitted model. The summary includes, for selected parameters, posterior medians and 95 percent credible intervals, the number of samples, the acceptance rate of the Markov chains, the effective number of independent samples and the Geweke convergence diagnostic in the form of a Z-score.

**Usage**

```
## S3 method for class 'CARBayesST'  
print(x, ...)
```

**Arguments**

<code>x</code>	A CARBayesST fitted model object.
<code>...</code>	Ignored.

**Author(s)**

Duncan Lee

---

`residuals.CARBayesST` *Extract the residuals from a model.*

---

### Description

This function takes a `CARBayesST` object and returns a set of residuals. The allowable types of residual are "response" (raw), and "pearson" (the default). In each case the fitted values are based on posterior means.

### Usage

```
## S3 method for class 'CARBayesST'
residuals(object, type, ...)
```

### Arguments

<code>object</code>	A <code>CARBayesST</code> fitted model object.
<code>type</code>	A text string and one of <code>c("response", "pearson")</code> . If this argument is omitted the default is "pearson".
<code>...</code>	Ignored.

### Author(s)

Duncan Lee

---

`ST.CARadaptive` *Fit a spatio-temporal generalised linear mixed model to data, with a spatio-temporal autoregressive process that has an adaptive autocorrelation structure.*

---

### Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial, Gaussian or Poisson. The linear predictor is modelled by known covariates and a vector of random effects. The latter follows a multivariate first order autoregressive time series process, where spatial autocorrelation is modelled via the precision matrix, which is based on a CAR type structure and a neighbourhood (adjacency) matrix  $W$ . The non-zero elements of  $W$  associated with each pair of geographically adjacent areal units are treated as random variables with ranges in the unit interval, which allows step changes to be identified in the random effects surface between geographically adjacent regions. The model is similar to that proposed by Rushworth et al. (2017). Further details are given in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

**Usage**

```
ST.CARadaptive(formula, family, data=NULL, trials=NULL, W, burnin, n.sample, thin=1,
prior.mean.beta=NULL, prior.var.beta=NULL, prior.nu2=NULL, prior.tau2=NULL,
rho = NULL, epsilon = 0, MALA=TRUE, verbose=TRUE)
```

**Arguments**

formula	A formula for the covariate part of the model using the syntax of the <code>lm()</code> function. Offsets can be included here using the <code>offset()</code> function. The response and each covariate should be vectors of length $(KN)*1$ , where $K$ is the number of spatial units and $N$ is the number of time periods. Each vector should be ordered so that the first $K$ data points are the set of all $K$ spatial locations at time 1, the next $K$ are the set of spatial locations for time 2 and so on. The response must NOT contain missing (NA) values.
family	One of either "binomial", "gaussian", or "poisson", which respectively specify a binomial likelihood model with a logistic link function, a Gaussian likelihood model with an identity link function, or a Poisson likelihood model with a log link function.
data	An optional data.frame containing the variables in the formula.
trials	A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial".
W	A non-negative $K$ by $K$ neighbourhood matrix (where $K$ is the number of spatial units). Typically a binary specification is used, where the $jk$ th element equals one if areas $(j, k)$ are spatially close (e.g. share a common border) and is zero otherwise. For this model the matrix must be binary.
burnin	The number of MCMC samples to discard as the burn-in period.
n.sample	The number of MCMC samples to generate.
thin	The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).
prior.mean.beta	A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros.
prior.var.beta	A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000.
prior.nu2	The prior shape and scale in the form of $c(\text{shape}, \text{scale})$ for an Inverse-Gamma(shape, scale) prior for nu2. Defaults to $c(1, 0.01)$ and only used if family="Gaussian".
prior.tau2	The prior shape and scale in the form of $c(\text{shape}, \text{scale})$ for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to $c(1, 0.01)$ .
rho	The value in the interval $[0, 1]$ that the spatial dependence parameter rho is fixed at if it should not be estimated. If this argument is NULL then rho is estimated in the model. Setting rho=1, reduces the random effects prior to the intrinsic CAR model but does require epsilon>0.
epsilon	Diagonal ridge parameter to add to the random effects prior precision matrix, only required when rho = 1, and the prior precision is improper. Defaults to 0.

MALA	Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) updates (TRUE, default) or simple random walk (FALSE) updates for the random effects. Not applicable if family="gaussian".
verbose	Logical, should the function update the user on its progress.

**Value**

summary.results	A summary table of the parameters.
samples	A list containing the MCMC samples from the model.
fitted.values	A vector of fitted values for each area and time period.
residuals	A matrix with 2 columns where each column is a type of residual and each row relates to an area and time period. The types are "response" (raw), and "pearson".
modelfit	Model fit criteria including the Deviance Information Criterion (DIC) and its corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the loglikelihood.
accept	The acceptance probabilities for the parameters.
localised.structure	A list with 2 K*K matrices, Wmedian and W99 summarising the estimated adjacency relationships. Wmedian contains the posterior median for each w_ij element estimated in the model for adjacent areal units, while W99 contains binary indicator variables for whether Prob(w_ij < 0.5 data)>0.99. For both matrices, elements corresponding to non-adjacent pairs of areas have NA values.
formula	The formula for the covariate and offset parts of the model.
model	A text string describing the model fit.
X	The design matrix of covariates.

**Author(s)**

Alastair Rushworth

**References**

Rushworth, A., Lee, D., and Sarran, C (2017). An adaptive spatio-temporal smoothing model for estimating trends and step changes in disease risk. *Journal of the Royal Statistical Society Series C*, 66, 141-157.

**Examples**

```
#####
#### Run the model on simulated data on a lattice
#####
#### set up the regular lattice
x.easting <- 1:10
```

```

x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)
K <- nrow(Grid)
N <- 10
N.all <- N * K

#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))
W <-array(0, c(K,K))
W[distance==1] <-1

#### Simulate the elements in the linear predictor and the data
Q.W <- 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi.temp <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))
phi <- phi.temp
  for(i in 2:N)
  {
    phi.temp2 <- mvrnorm(n=1, mu=(0.8 * phi.temp), Sigma=(0.1 * Q.W.inv))
    phi.temp <- phi.temp2
    phi <- c(phi, phi.temp)
  }
jump <- rep(c(rep(2, 70), rep(4, 30)),N)
LP <- jump + phi
fitted <- exp(LP)
Y <- rpois(n=N.all, lambda=fitted)

#### Run the model
## Not run: model <- ST.CARadaptive(formula=Y~1, family="poisson", W=W, burnin=10000,
n.sample=50000)
## End(Not run)

#### Toy example for checking
model <- ST.CARadaptive(formula=Y~1, family="poisson", W=W, burnin=10,
n.sample=50)

```

---

ST.CARanova

*Fit a spatio-temporal generalised linear mixed model to data, with spatial and temporal main effects and a spatio-temporal interaction.*


---

### Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial, Gaussian or Poisson. The linear predictor is modelled by known covariates and three vectors of random effects. The latter include spatial and temporal main effects and a spatio-temporal interaction. The spatial and temporal main effects are modelled by the conditional

autoregressive (CAR) prior proposed by Leroux et al. (2000), while the spatio-temporal interaction random effects are independent. Due to the lack of identifiability between the interactions and the Gaussian errors, only main effects are allowed in the Gaussian model. Missing values are allowed in the response in this model, and are sampled from in the model using data augmentation. The model is similar to that proposed by Knorr-Held (2000), and further details are given in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

## Usage

```
ST.CARanova(formula, family, data=NULL, trials=NULL, W, interaction=TRUE, burnin,
n.sample, thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.nu2=NULL,
prior.tau2=NULL, rho.S=NULL, rho.T=NULL, MALA=TRUE, verbose=TRUE)
```

## Arguments

formula	A formula for the covariate part of the model using the syntax of the <code>lm()</code> function. Offsets can be included here using the <code>offset()</code> function. The response and each covariate should be vectors of length $(KN)*1$ , where $K$ is the number of spatial units and $N$ is the number of time periods. Each vector should be ordered so that the first $K$ data points are the set of all $K$ spatial locations at time 1, the next $K$ are the set of spatial locations for time 2 and so on. The response can contain missing (NA) values.
family	One of either "binomial", "gaussian" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, a Gaussian likelihood model with an identity link function, or a Poisson likelihood model with a log link function.
data	An optional data.frame containing the variables in the formula.
trials	A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial".
W	A non-negative $K$ by $K$ neighbourhood matrix (where $K$ is the number of spatial units). Typically a binary specification is used, where the $jk$ th element equals one if areas $(j, k)$ are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry.
interaction	TRUE or FALSE indicating whether the spatio-temporal interaction random effects should be included. Defaults to TRUE unless family="gaussian" in which case interactions are not allowed.
burnin	The number of MCMC samples to discard as the burn-in period.
n.sample	The number of MCMC samples to generate.
thin	The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).
prior.mean.beta	A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros.

<code>prior.var.beta</code>	A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000.
<code>prior.nu2</code>	The prior shape and scale in the form of $c(\text{shape}, \text{scale})$ for an Inverse-Gamma(shape, scale) prior for nu2. Defaults to $c(1, 0.01)$ and only used if family="Gaussian".
<code>prior.tau2</code>	The prior shape and scale in the form of $c(\text{shape}, \text{scale})$ for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to $c(1, 0.01)$ .
<code>rho.S</code>	The value in the interval [0, 1] that the spatial dependence parameter rho.S is fixed at if it should not be estimated. If this argument is NULL then rho.S is estimated in the model.
<code>rho.T</code>	The value in the interval [0, 1] that the temporal dependence parameter rho.T is fixed at if it should not be estimated. If this argument is NULL then rho.T is estimated in the model.
<code>MALA</code>	Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) updates (TRUE, default) or simple random walk (FALSE) updates for the random effects. Not applicable if family="gaussian".
<code>verbose</code>	Logical, should the function update the user on its progress.

**Value**

<code>summary.results</code>	A summary table of the parameters.
<code>samples</code>	A list containing the MCMC samples from the model.
<code>fitted.values</code>	A vector of fitted values for each area and time period.
<code>residuals</code>	A matrix with 2 columns where each column is a type of residual and each row relates to an area and time period. The types are "response" (raw), and "pearson".
<code>modelfit</code>	Model fit criteria including the Deviance Information Criterion (DIC) and its corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the loglikelihood.
<code>accept</code>	The acceptance probabilities for the parameters.
<code>localised.structure</code>	NULL, for compatability with the other models.
<code>formula</code>	The formula for the covariate and offset parts of the model.
<code>model</code>	A text string describing the model fit.
<code>X</code>	The design matrix of covariates.

**Author(s)**

Duncan Lee

## References

Knorr-Held, L. (2000). Bayesian modelling of inseparable space-time variation in disease risk. *Statistics in Medicine*, 19, 2555-2567.

Leroux, B., X. Lei, and N. Breslow (2000). Estimation of disease rates in small areas: A new mixed model for spatial dependence, Chapter *Statistical Models in Epidemiology, the Environment and Clinical Trials*, Halloran, M and Berry, D (eds), pp. 135-178. Springer-Verlag, New York.

## Examples

```
#####
#### Run the model on simulated data on a lattice
#####
#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)
K <- nrow(Grid)
N <- 10
N.all <- N * K

#### set up spatial (W) and temporal (D) neighbourhood matrices
distance <- as.matrix(dist(Grid))
W <- array(0, c(K,K))
W[distance==1] <-1

D <- array(0, c(N,N))
for(i in 1:N)
{
  for(j in 1:N)
  {
    if(abs((i-j))==1) D[i,j] <- 1
  }
}

#### Simulate the elements in the linear predictor and the data
gamma <- rnorm(n=N.all, mean=0, sd=0.001)
x <- rnorm(n=N.all, mean=0, sd=1)
beta <- 0.1

Q.W <- 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))

Q.D <- 0.99 * (diag(apply(D, 2, sum)) - D) + 0.01 * diag(rep(1,N))
Q.D.inv <- solve(Q.D)
delta <- mvrnorm(n=1, mu=rep(0,N), Sigma=(0.01 * Q.D.inv))

phi.long <- rep(phi, N)
delta.long <- kronecker(delta, rep(1,K))
```

```

LP <- 4 + x * beta + phi.long + delta.long + gamma
mean <- exp(LP)
Y <- rpois(n=N.all, lambda=mean)

#### Run the model
## Not run: model <- ST.CARanova(formula=Y~x, family="poisson", interaction=TRUE,
W=W, burnin=10000, n.sample=50000)
## End(Not run)

#### Toy example for checking
model <- ST.CARanova(formula=Y~x, family="poisson", interaction=TRUE,
W=W, burnin=10, n.sample=50)

```

---

ST.CARar

*Fit a spatio-temporal generalised linear mixed model to data, with a spatio-temporal autoregressive process.*


---

## Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial, Gaussian or Poisson. The linear predictor is modelled by known covariates and a vector of random effects. The latter follows a multivariate first order autoregressive time series process, where spatial autocorrelation is modelled via the precision matrix. This precision matrix comes from the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000), and the full model was proposed by Rushworth et al. (2014). Missing values are allowed in the response in this model, and are sampled from in the model using data augmentation.. Further details are given in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

## Usage

```

ST.CARar(formula, family, data=NULL, trials=NULL, W, burnin, n.sample, thin=1,
prior.mean.beta=NULL, prior.var.beta=NULL, prior.nu2=NULL, prior.tau2=NULL,
rho.S=NULL, rho.T=NULL, MALA=TRUE, verbose=TRUE)

```

## Arguments

**formula** A formula for the covariate part of the model using the syntax of the `lm()` function. Offsets can be included here using the `offset()` function. The response and each covariate should be vectors of length  $(KN)*1$ , where  $K$  is the number of spatial units and  $N$  is the number of time periods. Each vector should be ordered so that the first  $K$  data points are the set of all  $K$  spatial locations at time 1, the next  $K$  are the set of spatial locations for time 2 and so on. The response can contain missing (NA) values.

family	One of either "binomial", "gaussian" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, a Gaussian likelihood model with an identity link function, or a Poisson likelihood model with a log link function.
data	An optional data.frame containing the variables in the formula.
trials	A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial".
W	A non-negative K by K neighbourhood matrix (where K is the number of spatial units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry.
burnin	The number of MCMC samples to discard as the burn-in period.
n.sample	The number of MCMC samples to generate.
thin	The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).
prior.mean.beta	A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros.
prior.var.beta	A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000.
prior.nu2	The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, scale) prior for nu2. Defaults to c(1, 0.01) and only used if family="Gaussian".
prior.tau2	The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to c(1, 0.01).
rho.S	The value in the interval [0, 1] that the spatial dependence parameter rho.S is fixed at if it should not be estimated. If this argument is NULL then rho.S is estimated in the model.
rho.T	The value in the interval [0, 1] that the temporal dependence parameter rho.T is fixed at if it should not be estimated. If this argument is NULL then rho.T is estimated in the model.
MALA	Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) updates (TRUE, default) or simple random walk (FALSE) updates for the random effects. Not applicable if family="gaussian".
verbose	Logical, should the function update the user on its progress.

### Value

summary.results	A summary table of the parameters.
samples	A list containing the MCMC samples from the model.
fitted.values	A vector of fitted values for each area and time period.

residuals	A matrix with 2 columns where each column is a type of residual and each row relates to an area and time period. The types are "response" (raw), and "pearson".
modelfit	Model fit criteria including the Deviance Information Criterion (DIC) and its corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the loglikelihood.
accept	The acceptance probabilities for the parameters.
localised.structure	NULL, for compatability with the other models.
formula	The formula for the covariate and offset parts of the model.
model	A text string describing the model fit.
X	The design matrix of covariates.

### Author(s)

Duncan Lee

### References

Rushworth, A., D. Lee, and R. Mitchell (2014). A spatio-temporal model for estimating the long-term effects of air pollution on respiratory hospital admissions in Greater London. *Spatial and Spatio-temporal Epidemiology* 10, 29-38.

### Examples

```
#####
#### Run the model on simulated data on a lattice
#####
#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)
K <- nrow(Grid)
N <- 10
N.all <- N * K

#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))
W <- array(0, c(K,K))
W[distance==1] <-1

#### Simulate the elements in the linear predictor and the data
gamma <- rnorm(n=N.all, mean=0, sd=0.001)
x <- rnorm(n=N.all, mean=0, sd=1)
beta <- 0.1
```

```

Q.W <- 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi.temp <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))
phi <- phi.temp
  for(i in 2:N)
  {
    phi.temp2 <- mvrnorm(n=1, mu=(0.8 * phi.temp), Sigma=(0.1 * Q.W.inv))
    phi.temp <- phi.temp2
    phi <- c(phi, phi.temp)
  }

LP <- 3 + x * beta + phi
mean <- exp(LP)
Y <- rpois(n=N.all, lambda=mean)

#### Run the model
## Not run: model <- ST.CARar(formula=Y~x, family="poisson", W=W, burnin=10000,
  n.sample=50000)
## End(Not run)

#### Toy example for checking
model <- ST.CARar(formula=Y~x, family="poisson", W=W, burnin=10,
  n.sample=50)

```

---

ST.CARclustrends	<i>Fit a spatio-temporal generalised linear mixed model to data, with a clustering of temporal trend functions and a temporally common spatial surface.</i>
------------------	---

---

## Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial or Poisson. The linear predictor is modelled by known covariates, a temporally common spatial surface, and a mixture of temporal trend functions. The spatial component is modelled by the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000). The temporal trend functions are user-specified and are fixed parametric forms (e.g. linear, step-change) or constrained shapes (e.g. monotonically increasing). Further details are given in Napier et al. (2018) and in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Metropolis coupled Markov chain Monte Carlo (MCMCMC) simulation.

## Usage

```

ST.CARclustrends(formula, family, data=NULL, trials=NULL, W, burnin, n.sample,
  thin=1, trends=NULL, changepoint=NULL, knots=NULL, prior.mean.beta=NULL,
  prior.var.beta=NULL, prior.mean.gamma=NULL, prior.var.gamma=NULL,
  prior.lambda=NULL, prior.tau2=NULL, Nchains=4, verbose=TRUE)

```

**Arguments**

formula	A formula using the syntax of the <code>lm()</code> function. However, due to identifiability issues covariates are not allowed. So the only elements allowed on the right side of the formula are an intercept term and an offset term using the <code>offset()</code> function. The response variable and the offset (if specified) should be vectors of length $(KN)*1$ , where $K$ is the number of spatial units and $N$ is the number of time periods. Each vector should be ordered so that the first $K$ data points are the set of all $K$ spatial locations at time 1, the next $K$ are the set of spatial locations for time 2 and so on.
family	One of either "binomial" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, or a Poisson likelihood model with a log link function.
data	An optional <code>data.frame</code> containing the variables in the formula.
trials	A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if <code>family="binomial"</code> .
W	A non-negative $K$ by $K$ neighbourhood matrix (where $K$ is the number of spatial units). Typically a binary specification is used, where the $jk$ th element equals one if areas $(j, k)$ are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry.
burnin	The number of MCMC samples to discard as the burn-in period.
n.sample	The number of MCMC samples to generate.
thin	The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).
trends	A vector containing the temporal trend functions to include in the model, which include: constant ("Constant"); linear decreasing ("LD"); linear increasing ("LI"); Known change point, where the trend can increase towards the change point before subsequently decreasing ("CP"); or decrease towards the change point before subsequently increasing ("CT"); and monotonic cubic splines which are decreasing ("MD") or increasing ("MI"). At least two trends have to be selected, with the constant trend always included. To avoid identifiability problems only one of "LI" or "MI" can be included at a given time (similarly for "LD" and "MD").
change point	A scalar indicating the position of the change point should one of the change point trend functions be included in the trends vector, i.e. if "CP" or "CT" is specified.
knots	A scalar indicating the number of knots to use should one of the monotonic cubic splines trend functions be included in the trends vector, i.e. if "MD" or "MI" is specified.
prior.mean.beta	A vector of prior means for the regression parameters $\beta$ (Gaussian priors are assumed). Defaults to a vector of zeros.
prior.var.beta	A vector of prior variances for the regression parameters $\beta$ (Gaussian priors are assumed). Defaults to a vector with values 100000.

<code>prior.mean.gamma</code>	A vector of prior means for the temporal trend parameters (Gaussian priors are assumed). Defaults to a vector of zeros.
<code>prior.var.gamma</code>	A vector of prior variances for the temporal trend parameters (Gaussian priors are assumed). Defaults to a vector with values 100000.
<code>prior.lambda</code>	A vector of prior samples sizes for the Dirichlet prior controlling the probabilities that each trend function is chosen. The vector should be the same length as the trends vector and defaults to a vector of ones.
<code>prior.tau2</code>	The prior shape and scale in the form of $c(\text{shape}, \text{scale})$ for an Inverse-Gamma(shape, scale) prior for the random effect variances tau2. Defaults to $c(1, 0.01)$ .
<code>Nchains</code>	The number of parallel Markov chains to be used in the Metropolis coupled Markov chain Monte Carlo (MCMCMC) simulations. Defaults to 4.
<code>verbose</code>	Logical, should the function update the user on its progress.

**Value**

<code>summary.results</code>	A summary table of the parameters.
<code>samples</code>	A list containing the MCMC samples from the model.
<code>fitted.values</code>	A vector of fitted values for each area and time period.
<code>residuals</code>	A matrix with 2 columns where each column is a type of residual and each row relates to an area and time period. The types are "response" (raw), and "pearson".
<code>modelfit</code>	Model fit criteria including the Deviance Information Criterion (DIC) and its corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the loglikelihood.
<code>accept</code>	The acceptance probabilities for the parameters.
<code>localised.structure</code>	A list containing two elements. The first is "trends", which is a vector the same length and in the same order as the number of areas. The kth element specifies which trend area k has been allocated to based on the posterior mode. The second element is "trend.probs", which is a matrix containing the probabilities associated with each trend for each areal unit.
<code>formula</code>	The formula for the covariate and offset parts of the model.
<code>model</code>	A text string describing the model fit.
<code>X</code>	The design matrix of covariates.

**Author(s)**

Gary Napier

## References

Leroux, B., Lei, X., and Breslow, N. (2000). Estimation of disease rates in small areas: A new mixed model for spatial dependence, Chapter Statistical Models in Epidemiology, the Environment and Clinical Trials, Halloran, M and Berry, D (eds), pp. 135-178. Springer-Verlag, New York.

Napier, G., Lee, D., Robertson, C., and Lawson, A. (2018). A Bayesian space-time model for clustering areal units based on their disease trends, *Biostatistics*, to appear, 10.1093/biostatistics/kxy024.

## Examples

```
#####
#### Run the model on simulated data on a lattice
#####
#### Load the libraries required
library(truncdist)
library(gtools)

#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)
K <- nrow(Grid)
N <- 10
N.all <- N * K

#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))
W <- array(0, c(K,K))
W[distance==1] <-1

#### Create the spatial covariance matrix
Q.W <- 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)

#### Simulate the elements in the linear predictor and the data
beta <- 0.01
gamma <- 0.7
phi <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))

lambda <- rep(1/2, 2)
w <- t(rmultinom(K, 1, lambda))

Y <- matrix(NA, nrow = K, ncol = N)
for (i in 1:N)
{
  LP <- beta + w[, 2] * (gamma * i) + phi
  mean <- exp(LP)
  Y[, i] <- rpois(n=K, lambda=mean)
}
```

```

Y <- as.numeric(Y)

#### Run the model
## Not run: model <- ST.CARclustrends(formula=Y~1, family="poisson", W=W, burnin=10000,
n.sample=50000, trends=c("Constant", "LI"))
## End(Not run)

#### Toy example for checking
model <- ST.CARclustrends(formula=Y~1, family="poisson", W=W, burnin=10,
n.sample=50, trends=c("Constant", "LI"))

```

---

ST.CARlinear	<i>Fit a spatio-temporal generalised linear mixed model to data, where the spatial units have linear time trends with spatially varying intercepts and slopes.</i>
--------------	--

---

## Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial, Gaussian or Poisson. The linear predictor is modelled by known covariates and an area specific linear time trend. The area specific intercepts and slopes are spatially autocorrelated and modelled by the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000). The model is similar to that proposed by Bernardinelli et al. (1995) and further details are given in the vignette accompanying this package. Missing values are allowed in the response in this model, and are sampled from in the model using data augmentation. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

## Usage

```

ST.CARlinear(formula, family, data=NULL, trials=NULL, W, burnin, n.sample, thin=1,
prior.mean.beta=NULL, prior.var.beta=NULL, prior.mean.alpha=NULL,
prior.var.alpha=NULL, prior.nu2=NULL, prior.tau2=NULL, rho.slo=NULL, rho.int=NULL,
MALA=TRUE, verbose=TRUE)

```

## Arguments

formula	A formula for the covariate part of the model using the syntax of the <code>lm()</code> function. Offsets can be included here using the <code>offset()</code> function. The response and each covariate should be vectors of length $(KN)*1$ , where $K$ is the number of spatial units and $N$ is the number of time periods. Each vector should be ordered so that the first $K$ data points are the set of all $K$ spatial locations at time 1, the next $K$ are the set of spatial locations for time 2 and so on. The response can contain missing (NA) values.
family	One of either "binomial", "gaussian" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, a Gaussian likelihood model with an identity link function, or a Poisson likelihood model with a log link function.

<code>data</code>	An optional data.frame containing the variables in the formula.
<code>trials</code>	A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial".
<code>W</code>	A non-negative K by K neighbourhood matrix (where K is the number of spatial units). Typically a binary specification is used, where the jkth element equals one if areas (j, k) are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry.
<code>burnin</code>	The number of MCMC samples to discard as the burn-in period.
<code>n.sample</code>	The number of MCMC samples to generate.
<code>thin</code>	The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).
<code>prior.mean.beta</code>	A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros.
<code>prior.var.beta</code>	A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000.
<code>prior.mean.alpha</code>	The prior mean for the average slope of the linear time trend alpha (a Gaussian prior is assumed). Defaults to zero.
<code>prior.var.alpha</code>	The prior variance for the average slope of the linear time trend alpha (a Gaussian prior is assumed). Defaults to 100000.
<code>prior.nu2</code>	The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, scale) prior for nu2. Defaults to c(1, 0.01) and only used if family="Gaussian".
<code>prior.tau2</code>	The prior shape and scale in the form of c(shape, scale) for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to c(1, 0.01).
<code>rho.slo</code>	The value in the interval [0, 1] that the spatial dependence parameter for the slope of the linear time trend, rho.slo, is fixed at if it should not be estimated. If this argument is NULL then rho.slo is estimated in the model.
<code>rho.int</code>	The value in the interval [0, 1] that the spatial dependence parameter for the intercept of the linear time trend, rho.int, is fixed at if it should not be estimated. If this argument is NULL then rho.int is estimated in the model.
<code>MALA</code>	Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) updates (TRUE, default) or simple random walk (FALSE) updates for the random effects. Not applicable if family="gaussian".
<code>verbose</code>	Logical, should the function update the user on its progress.

**Value**

<code>summary.results</code>	A summary table of the parameters.
<code>samples</code>	A list containing the MCMC samples from the model.

fitted.values	A vector of fitted values for each area and time period.
residuals	A matrix with 2 columns where each column is a type of residual and each row relates to an area and time period. The types are "response" (raw), and "pearson".
modelfit	Model fit criteria including the Deviance Information Criterion (DIC) and its corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the loglikelihood.
accept	The acceptance probabilities for the parameters.
localised.structure	NULL, for compatability with the other models.
formula	The formula for the covariate and offset parts of the model.
model	A text string describing the model fit.
X	The design matrix of covariates.

**Author(s)**

Duncan Lee

**References**

Bernardinelli, L., D. Clayton, C.Pascuto, C.Montomoli, M.Ghislandi, and M. Songini (1995). Bayesian analysis of space-time variation in disease risk. *Statistics in Medicine*, 14, 2433-2443.

Leroux, B., X. Lei, and N. Breslow (2000). Estimation of disease rates in small areas: A new mixed model for spatial dependence, Chapter *Statistical Models in Epidemiology, the Environment and Clinical Trials*, Halloran, M and Berry, D (eds), pp. 135-178. Springer-Verlag, New York.

**Examples**

```
#####
#### Run the model on simulated data on a lattice
#####
#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)
K <- nrow(Grid)
N <- 10
N.all <- K * N

#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))
W <- array(0, c(K,K))
W[distance==1] <-1
```

```

#### Simulate the elements in the linear predictor and the data
x <- rnorm(n=N.all, mean=0, sd=1)
beta <- 0.1
Q.W <- 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))
delta <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))
trend <- array(NA, c(K, N))
time <- (1:N - mean(1:N))/N
  for(i in 1:K)
  {
    trend[i, ] <- phi[i] + delta[i] * time
  }
trend.vec <- as.numeric(trend)
LP <- 4 + x * beta + trend.vec
mean <- exp(LP)
Y <- rpois(n=N.all, lambda=mean)

#### Run the model
## Not run: model <- ST.CARlinear(formula=Y~x, family="poisson", W=W, burnin=10000,
n.sample=50000)
## End(Not run)

#### Toy example for checking
model <- ST.CARlinear(formula=Y~x, family="poisson", W=W, burnin=10,
n.sample=50)

```

---

ST.CARlocalised

*Fit a spatio-temporal generalised linear mixed model to data, with a spatio-temporal autoregressive process and a piecewise constant intercept term.*

---

## Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial or Poisson. The linear predictor is modelled by known covariates, a vector of random effects and a piecewise constant intercept process. The random effects follow the multivariate first order autoregressive time series process proposed by Rushworth et al.(2014), which is the same as that used in the ST.CARar() function. The piecewise constant intercept component allows neighbouring areal units to have very different values if they are assigned to a different intercept component. This model allows for localised smoothness, because some pairs of neighbouring areas or time periods can have similar values (same intercept) while other neighbouring pairs have very different values (different intercepts). Further details are given in Lee and Lawson (2016) and in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

**Usage**

```
ST.CARlocalised(formula, family, data=NULL, G, trials=NULL, W, burnin, n.sample,
thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.delta=NULL,
prior.tau2=NULL, MALA=TRUE, verbose=TRUE)
```

**Arguments**

formula	A formula for the covariate part of the model using the syntax of the <code>lm()</code> function. Offsets can be included here using the <code>offset()</code> function. The response and each covariate should be vectors of length $(KN)*1$ , where $K$ is the number of spatial units and $N$ is the number of time periods. Each vector should be ordered so that the first $K$ data points are the set of all $K$ spatial locations at time 1, the next $K$ are the set of spatial locations for time 2 and so on. The response must NOT contain missing (NA) values.
family	One of either "binomial", or "poisson", which respectively specify a binomial likelihood model with a logistic link function, or a Poisson likelihood model with a log link function.
data	An optional data.frame containing the variables in the formula.
G	The maximum number of distinct intercept terms (clusters) to allow in the model.
trials	A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial".
W	A non-negative $K$ by $K$ neighbourhood matrix (where $K$ is the number of spatial units). Typically a binary specification is used, where the $jk$ th element equals one if areas $(j, k)$ are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry.
burnin	The number of MCMC samples to discard as the burn-in period.
n.sample	The number of MCMC samples to generate.
thin	The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).
prior.mean.beta	A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros.
prior.var.beta	A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000.
prior.delta	The prior maximum $M$ , in a Uniform(0, $M$ ) prior, for the intercept process smoothing parameter delta. Defaults to 10.
prior.tau2	The prior shape and scale in the form of $c(\text{shape}, \text{scale})$ for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to $c(1, 0.01)$ .
MALA	Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) updates (TRUE, default) or simple random walk (FALSE) updates for the random effects. Not applicable if family="gaussian".
verbose	Logical, should the function update the user on its progress.

**Value**

summary.results	A summary table of the parameters.
samples	A list containing the MCMC samples from the model.
fitted.values	A vector of fitted values for each area and time period.
residuals	A matrix with 2 columns where each column is a type of residual and each row relates to an area and time period. The types are "response" (raw), and "pearson".
modelfit	Model fit criteria including the Deviance Information Criterion (DIC) and its corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the loglikelihood.
accept	The acceptance probabilities for the parameters.
localised.structure	A vector giving the posterior mean of which intercept component (cluster) each data point is in.
formula	The formula for the covariate and offset parts of the model.
model	A text string describing the model fit.
X	The design matrix of covariates.

**Author(s)**

Duncan Lee

**References**

Lee, D and Lawson, C (2016). Quantifying the spatial inequality and temporal trends in maternal smoking rates in Glasgow, *Annals of Applied Statistics*, 10, 1427-1446.

**Examples**

```
#####
#### Run the model on simulated data on a lattice
#####
#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)
K <- nrow(Grid)
N <- 10
N.all <- N * K

#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))
W <-array(0, c(K,K))
```

```

W[distance==1] <-1

#### Simulate the elements in the linear predictor and the data
Q.W <- 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)
phi.temp <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.1 * Q.W.inv))
phi <- phi.temp
  for(i in 2:N)
  {
    phi.temp2 <- mvrnorm(n=1, mu=(0.8 * phi.temp), Sigma=(0.1 * Q.W.inv))
    phi.temp <- phi.temp2
    phi <- c(phi, phi.temp)
  }
jump <- rep(c(rep(2, 70), rep(4, 30)),N)
LP <- jump + phi
fitted <- exp(LP)
Y <- rpois(n=N.all, lambda=fitted)

#### Run the model
## Not run: model <- ST.CARlocalised(formula=Y~1, family="poisson", G=3, W=W, burnin=10000,
n.sample=50000)
## End(Not run)

#### Toy example for checking
model <- ST.CARlocalised(formula=Y~1, family="poisson", G=3, W=W, burnin=10,
n.sample=50)

```

---

ST.CARsepspatial	<i>Fit a spatio-temporal generalised linear mixed model to data, with a common temporal main effect and separate spatial surfaces with individual variances.</i>
------------------	--

---

## Description

Fit a spatio-temporal generalised linear mixed model to areal unit data, where the response variable can be binomial or Poisson. The linear predictor is modelled by known covariates and two sets of random effects. These include a common temporal main effect, and separate time period specific spatial effects with a common spatial dependence parameter but separate variance parameters. Each component is modelled by the conditional autoregressive (CAR) prior proposed by Leroux et al. (2000). Further details are given in Napier et al. (2016) and in the vignette accompanying this package. Inference is conducted in a Bayesian setting using Markov chain Monte Carlo (MCMC) simulation.

## Usage

```

ST.CARsepspatial(formula, family, data=NULL, trials=NULL, W, burnin, n.sample,
thin=1, prior.mean.beta=NULL, prior.var.beta=NULL, prior.tau2=NULL, rho.S=NULL,
rho.T=NULL, MALA=TRUE, verbose=TRUE)

```

**Arguments**

formula	A formula for the covariate part of the model using the syntax of the <code>lm()</code> function. Offsets can be included here using the <code>offset()</code> function. The response and each covariate should be vectors of length $(KN)*1$ , where $K$ is the number of spatial units and $N$ is the number of time periods. Each vector should be ordered so that the first $K$ data points are the set of all $K$ spatial locations at time 1, the next $K$ are the set of spatial locations for time 2 and so on. The response must NOT contain missing (NA) values.
family	One of either "binomial" or "poisson", which respectively specify a binomial likelihood model with a logistic link function, or a Poisson likelihood model with a log link function.
data	An optional data.frame containing the variables in the formula.
trials	A vector the same length and in the same order as the response containing the total number of trials for each area and time period. Only used if family="binomial".
W	A non-negative $K$ by $K$ neighbourhood matrix (where $K$ is the number of spatial units). Typically a binary specification is used, where the $jk$ th element equals one if areas $(j, k)$ are spatially close (e.g. share a common border) and is zero otherwise. The matrix can be non-binary, but each row must contain at least one non-zero entry.
burnin	The number of MCMC samples to discard as the burn-in period.
n.sample	The number of MCMC samples to generate.
thin	The level of thinning to apply to the MCMC samples to reduce their temporal autocorrelation. Defaults to 1 (no thinning).
prior.mean.beta	A vector of prior means for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector of zeros.
prior.var.beta	A vector of prior variances for the regression parameters beta (Gaussian priors are assumed). Defaults to a vector with values 100000.
prior.tau2	The prior shape and scale in the form of $c(\text{shape}, \text{scale})$ for an Inverse-Gamma(shape, scale) prior for tau2. Defaults to $c(1, 0.01)$ .
rho.S	The value in the interval $[0, 1]$ that the spatial dependence parameter rho.S is fixed at if it should not be estimated. If this argument is NULL then rho.S is estimated in the model.
rho.T	The value in the interval $[0, 1]$ that the temporal dependence parameter rho.T is fixed at if it should not be estimated. If this argument is NULL then rho.T is estimated in the model.
MALA	Logical, should the function use Metropolis adjusted Langevin algorithm (MALA) updates (TRUE, default) or simple random walk (FALSE) updates for the random effects. Not applicable if family="gaussian".
verbose	Logical, should the function update the user on its progress.

**Value**

summary.results	A summary table of the parameters.
samples	A list containing the MCMC samples from the model.
fitted.values	A vector of fitted values for each area and time period.
residuals	A matrix with 2 columns where each column is a type of residual and each row relates to an area and time period. The types are "response" (raw), and "pearson".
modelfit	Model fit criteria including the Deviance Information Criterion (DIC) and its corresponding estimated effective number of parameters (p.d), the Log Marginal Predictive Likelihood (LMPL), the Watanabe-Akaike Information Criterion (WAIC) and its corresponding estimated number of effective parameters (p.w), and the loglikelihood.
accept	The acceptance probabilities for the parameters.
localised.structure	NULL, for compatability with the other models.
formula	The formula for the covariate and offset parts of the model.
model	A text string describing the model fit.
X	The design matrix of covariates.

**Author(s)**

Gary Napier

**References**

Napier, G, D. Lee, C. Robertson, A. Lawson, and K. Pollock (2016). A model to estimate the impact of changes in MMR vaccination uptake on inequalities in measles susceptibility in Scotland, *Statistical Methods in Medical Research*, 25, 1185-1200.

**Examples**

```
#####
#### Run the model on simulated data on a lattice
#####
#### set up the regular lattice
x.easting <- 1:10
x.northing <- 1:10
Grid <- expand.grid(x.easting, x.northing)
K <- nrow(Grid)
N <- 5
N.all <- N * K

#### set up spatial neighbourhood matrix W
distance <- as.matrix(dist(Grid))
W <-array(0, c(K,K))
```

```
W[distance==1] <-1

#### Create the spatial covariance matrix
Q.W <- 0.99 * (diag(apply(W, 2, sum)) - W) + 0.01 * diag(rep(1,K))
Q.W.inv <- solve(Q.W)

#### Simulate the elements in the linear predictor and the data
x <- rnorm(n=N.all, mean=0, sd=1)
beta <- 0.1

phi1 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))
phi2 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))
phi3 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.01 * Q.W.inv))
phi4 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.05 * Q.W.inv))
phi5 <- mvrnorm(n=1, mu=rep(0,K), Sigma=(0.05 * Q.W.inv))

delta <- c(0, 0.5, 0, 0.5, 0)
phi.long <- c(phi1, phi2, phi3, phi4, phi5)
delta.long <- kronecker(delta, rep(1,K))
LP <- 4 + x * beta + phi.long + delta.long
mean <- exp(LP)
Y <- rpois(n=N.all, lambda=mean)

#### Run the model
## Not run: model <- ST.CARsepspatial(formula=Y~x, family="poisson", W=W, burnin=10000,
n.sample=50000)
## End(Not run)

#### Toy example for checking
model <- ST.CARsepspatial(formula=Y~x, family="poisson", W=W, burnin=10,
n.sample=50)
```

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